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# Disturbances Classification based on a Model Order Selection Method for Power Quality Monitoring

Zakarya Oubrahim, *Student Member, IEEE*, Vincent Choqueuse, *Member, IEEE*, Yassine Amirat, *Member, IEEE* and Mohamed Benbouzid, *Senior Member, IEEE*

**Abstract**—In this paper, a new technique for power quality disturbances classification is proposed. It focuses on voltage sags and swells that are first pre-classified into four classes that depend on the number of non-zero symmetrical components and can contain different types of sag and swell. Using the estimated symmetrical component values, we can afterward classify the corresponding sag or swell signature. In this study, we show that the pre-classification can be reformulated as a pure model order selection problem. To solve this problem, we propose two pre-classifiers based on Information Theoretical Criteria. The former yields the highest statistical performances, while the latter has a lower computation complexity. The performances of the proposed classification algorithms are evaluated using Monte Carlo simulations on synthetic signals and using real power system data obtained from the DOE/EPRI National Database of Power System Events. The achieved simulations and experimental results clearly illustrate the effectiveness of the proposed algorithms for voltage sag and swell classification.

**Index Terms**—Power quality monitoring, disturbances, voltage sags and swells, estimation, classification, symmetrical components, unbalanced power system.

## I. INTRODUCTION

OVER the last decades, the necessity of producing more energy combined with the interest in clean energies have led to a greater penetration of renewable energy systems in the power grid. The intermittent and discontinuous nature of renewable energy sources may impact the power system and can lead to grid instability or even its failure. Particularly, the integration of renewable energy sources has a substantial influence on power quality by affecting voltage and frequency control [1]–[4]. To overcome this difficulty, the need of a better control strategies for power systems have recently led to the concept of smart-grids [5]. A smart grid uses two-way flows of electricity and information, and computational intelligence in an integrated fashion across the entire spectrum of the energy system from the generation to the end points of electricity consumption [6]. A smart-grid is a modern electric power grid infrastructure for improved efficiency, reliability, and safety, through automated control and modern communication technologies. Furthermore, the future smart grid is expected to be self-healing and resilient to system anomalies [7]–[10].

A key role of a smart grid is allowing an electrical grid to be more flexible while meeting power quality standards. Power Quality (PQ) is a very significant issue of electrical power system operations. PQ disturbances can be extremely different in their characteristics and consequences for end-user equipments. They are usually divided into several classes such as sag, swell, transient,

fluctuation, and interruption [11]. Voltage sags and swells are one of the most critical disturbances in power supply because they can degrade customer load performance and efficiency. From an economic viewpoint, these disturbances can cause million-dollar losses for industrial consumers [12].

In terms of power quality issues, this paper focuses on voltage sags and swells. There are several international standards for characterizing voltage sags and swells, such as the IEEE 1159, IEC 61000-4-30, and EN 50160 [13]–[15]. According to the IEEE std. 1159, a sag is a decrease in the root mean square (rms) voltage or current levels from 0.1 to 0.9 per unit (pu) at the power system frequency for durations ranging from a half-cycle to one minute (short time), or over one minute (long time). According to the same standard, a swell is an increase in the rms voltage level between 1.1 and 1.8 pu of the nominal value. To minimize their economical impacts, it becomes imperative to integrate advanced algorithms to characterize voltage sags and swells. This characterization is usually composed of two steps which are the event detection, that is concerned with determining the starting and ending times of the event, and the event classification [11].

Several techniques have been proposed in the literature to detect three-phase unbalance and/or classify voltage sags and swells. Regarding the detection of three-phase unbalance, [16] and [17] describe two techniques based on hypothesis tests. The classification of PQ disturbances have also been investigated in [18]–[21], where two-voltage classification algorithms were proposed. These algorithms allow classifying the six voltage sag types  $C_a$ ,  $C_b$ ,  $C_c$ ,  $D_a$ ,  $D_b$ , and  $D_c$  according to the ABC classification proposed in [22]. The first classifier is based on symmetrical components (SC) and the second classifier is based on three-phase voltage magnitudes and their phase angles (TP-TAA). The classifier described in [19] and T18 compares the six rms values of phase-to-ground and phase-to-phase voltages after removing the zero-sequence component. This six-phase algorithm also classifies the voltage sag types  $C_a$ ,  $C_b$ ,  $C_c$ ,  $D_a$ ,  $D_b$ , and  $D_c$ . Despite their simplicity, these techniques are very sensitive to large variations in magnitude or phase-angle jump and they do not cover all sag types proposed in [22]. In [23], the authors have proposed a technique based on space vector representation in the complex plane and zero sequence voltage. This technique provides a complete sag and swell type classification. A fault detection and classification technique using wavelet transform (WT) has been also proposed in [24].

A panorama and state of the art of PQ disturbances classification based on pattern recognition techniques has been proposed in [29]. Classifiers based on pattern recognition techniques, such as artificial neural networks (ANN) or support vector machine (SVM), have been presented in [25]–[28]. In [30], a PQ disturbances classifier based on balanced neural tree method and using empirical-mode decomposition (EMD) has been presented. However, the EMD suffers from drawbacks such as mode mixing that may lead to a wrong intrinsic mode functions (IMF) decomposition, and border effects. In [31], the authors have proposed a PQ disturbances analysis method based on wavelets and fuzzy sets theory. Nevertheless, the

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wavelet transform technique leads to poor performances accuracy under noisy environment. In [32], a hybrid fuzzy C-means particle swarm optimization (PSO) technique has been proposed for PQ disturbances classification using a variety of windowing techniques. This technique uses the S-transform, which is an extension of the wavelet transform (WT). An approach for PQ disturbances detection and classification under non-stationary conditions based on S-transform and neural networks has also been presented in [33]. In [34], the authors have developed an S-transform-based probabilistic neural network (PNN) classifier for recognition of PQ disturbances. A combination of a neural-network-based technique for single and combined PQ disturbances detection and classification under noiseless and noisy conditions has been proposed in [35]. Although this classifier has good capabilities for classifying combined PQ disturbances, the analysis stage needs more attention about sub-classes of each PQ disturbance, especially sag and swell. A feature extraction method for the automatic classification of PQ disturbances based on wavelet neural network (WNN) has been proposed in [36]. Its main advantage is the reduction of training data size and a good signal characterization. A SVM classification system for voltage disturbances has been proposed in [37], where the SVM classifier performances is investigated for different training and testing data. However, the performances of all the above-presented artificial intelligence techniques critically depend on the learning stage that requires a training database. The size of this latter must be sufficiently large to encompass different kinds of power quality conditions, which may be difficult to obtain in practice. Their performances also depend on many parameters and on the features extraction process. Furthermore, the learning stage requires relatively high computational complexity effort. Moreover, most of previous works in PQ disturbance classification are suboptimal because they only exploit the information contained in a single-phase, instead of exploiting the multidimensional nature of the electrical signals [38].

To overcome these problems, this paper proposes a new PQ classification technique based on the analysis of the three-phase signal. The proposed classifier can be applied as a post-processing tool for transient characterization and disturbance detection in power systems [11]. Similarly to the technique described in [17], the proposed classifier is based on *model order selection*. Nevertheless, unlike the method in [17], which mainly focuses on the detection problem, the proposed technique emphasizes on the classification problem. Specifically, the proposed classifier is able to identify the number of non-zero symmetrical components and to pre-classify the signal into 4 classes under quasi-stationary conditions. Once the correct class is selected, the corresponding sag or swell can be identified using the estimated symmetrical components. The performances of the proposed algorithm are evaluated with synthetic and experimental data. Thus, an in-depth analysis of its sensitivity is carried out for different signal lengths, noisy environments, and quasi-stationary conditions. Then, its robustness is evaluated for different Total Harmonic Distortion (THD) values. After that, the classifier computation complexity is analyzed. Finally, a comparison is carried out between the proposed technique and two other classifiers, namely the symmetrical components and the three-phase three-angle algorithms.

The main contributions of this paper, with respect to the above-discussed literature, can be summarized as follows:

- Compared to the classifiers published in [18], [19], [21], the proposed algorithm has the ability to provide a complete sag and swell classification. In contrast to pattern recognition-based classifiers, the proposed algorithm does not require any training database and no parameter to be set. Furthermore, while most of the PQ disturbance classification techniques exploit single-phase

information, the proposed classifier will exploit three-phase information that allow better classification performances [29].

- A comparison between two proposed pre-classifiers based on Information Theoretical Criteria has been made. The first pre-classifier is called the Maximum Likelihood (ML) pre-classifier and the seconde one is called the Approximate (App) pre-classifier. The former yields the highest statistical performances, while the latter has a lower computation complexity. Then, a classifier based on estimated symmetrical component values has been proposed and evaluated. It allows the classification of the corresponding sag or swell.
- An experimental validation with time-varying real power system signals is carried out.

This paper is organized as follows. Section II presents the signal and phasor models. Section III describes the classification method for sags and swells signatures, then Section IV illustrates the effectiveness of the proposed technique evaluated using Monte Carlo simulations on synthetic signals and using real power system data.

## II. SIGNAL AND PHASOR MODELS

This section presents the three-phase signal and phasor models. Based on the phasor model, we also describe the 4-classes and the nine sags and swells signatures.

### A. Three-Phase Signals Model

In a three-phase power system, the signal on phase  $m$  ( $m = 0, 1, 2$ ) can be expressed as [39]

$$x_m[n] = a_m \cos(n\omega_0 + \varphi_m) + b_m[n], \quad (1)$$

where  $a_m$  and  $\varphi_m$  correspond to the amplitude and phase angle, respectively,  $\omega_0$  denotes the normalized angular frequency, and  $b_m[n]$  refers to the additive noise. The parameters  $a_m$  and  $\varphi_m$  are usually described more compactly by introducing the complex phasor. Mathematically, the complex phasor on phase  $m$  is defined as

$$c_m \triangleq a_m e^{j\varphi_m}. \quad (2)$$

Without loss of generality, we assume that the voltage sensors record  $N$  consecutive samples ( $n = 0, 1, \dots, N-1$ ). By using a matrix notation, the recorded samples on the three phases can be written as

$$\mathbf{X} = \mathbf{A}\mathbf{C} + \mathbf{B}, \quad (3)$$

where

- $\mathbf{X}$  and  $\mathbf{B}$  are  $N \times 3$  matrices containing the recorded and noise samples, respectively. These matrices are defined by

$$\mathbf{X} = \begin{bmatrix} x_0[0] & x_1[0] & x_2[0] \\ \vdots & \vdots & \vdots \\ x_0[N-1] & x_1[N-1] & x_2[N-1] \end{bmatrix}, \quad (4)$$

$$\mathbf{B} = \begin{bmatrix} b_0[0] & b_1[0] & b_2[0] \\ \vdots & \vdots & \vdots \\ b_0[N-1] & b_1[N-1] & b_2[N-1] \end{bmatrix}, \quad (5)$$

- $\mathbf{A}$  is a  $N \times 2$  real-valued matrix which is defined by

$$\mathbf{A} = \begin{bmatrix} 1 & 0 \\ \cos(w_0) & \sin(w_0) \\ \vdots & \vdots \\ \cos((N-1)w_0) & \sin((N-1)w_0) \end{bmatrix}, \quad (6)$$

- $\mathbf{C}$  is a  $2 \times 3$  real-valued matrix containing the real and imaginary parts of the phasors and is defined by

$$\mathbf{C} = \begin{bmatrix} a_0 \cos(\varphi_0) & a_1 \cos(\varphi_1) & a_2 \cos(\varphi_2) \\ -a_0 \sin(\varphi_0) & -a_1 \sin(\varphi_1) & -a_2 \sin(\varphi_2) \end{bmatrix}. \quad (7)$$

In the following, we resort to a vectorized version of  $\mathbf{X}$  to analyse the recorded signal. Let us introduce  $\text{vec}(\cdot)$  the vectorization operator that converts a matrix into a column vector by stacking the columns of the matrix on top of one another. Using the properties of the vectorization operator, the three-phase signal  $\mathbf{x} \triangleq \text{vec}(\mathbf{X})$  can be expressed into a  $3N \times 1$  column vector as

$$\mathbf{x} = (\mathbf{I}_3 \otimes \mathbf{A}) \mathbf{c} + \mathbf{b}, \quad (8)$$

where  $\mathbf{b} = \text{vec}(\mathbf{B})$ ,  $\mathbf{c} \triangleq \text{vec}(\mathbf{C})$ ,  $\mathbf{I}_3$  is the  $3 \times 3$  identity matrix, and  $\otimes$  corresponds to the Kronecker product.

### B. Phasor Model

In order to analyze the phasors configuration, it is usually convenient to decompose the three complex phasors into a more synthetic basis. In this subsection, we propose to decompose the three phasors  $c_0$ ,  $c_1$ , and  $c_2$  into a basis composed of 3 symmetrical components called the zero-sequence  $z_0$ , positive-sequence  $z_1$ , and negative-sequence  $z_2$ . The complex phasors  $c_1$ ,  $c_2$  and  $c_3$  can be expressed according to these three symmetrical components through the Fortescue transform as [40]

$$\begin{bmatrix} c_0 \\ c_1 \\ c_2 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & e^{4j\pi/3} & e^{2j\pi/3} \\ 1 & e^{2j\pi/3} & e^{4j\pi/3} \end{bmatrix} \begin{bmatrix} z_0 \\ z_1 \\ z_2 \end{bmatrix}. \quad (9)$$

The main benefit of using the symmetrical components relies on the fact that, under nominal conditions, the symmetrical components are sparse i.e.  $z_0 = z_2 = 0$ . In this paper, we consider the 4 following classes.

- $C_1$ : Zero and negative sequences are equal to 0 i.e.  $z_0 = z_2 = 0$ .
- $C_2$ : Zero sequence is equal to 0 i.e.  $z_0 = 0$ .
- $C_3$ : Negative sequence is equal to 0 i.e.  $z_2 = 0$ .
- $C_4$ : All sequences are different from 0.

For the 4 considered classes, the vector containing the real and imaginary parts of the three phasors,  $\mathbf{c}$ , in (8) can be expressed with respect to the real and imaginary parts of the symmetrical components as

$$\mathbf{c} = \mathbf{W}_k \mathbf{s}_k, \quad (10)$$

where the matrix  $\mathbf{W}_k$  and the *augmented* symmetrical components  $\mathbf{s}_k$  depend on the class number. For example, for Class  $C_1$ , the vector  $\mathbf{c}$  can be decomposed as

$$\mathbf{c} = \underbrace{\begin{bmatrix} \mathbf{Q}_0 \\ \mathbf{Q}_1 \\ \mathbf{Q}_2 \end{bmatrix}}_{\mathbf{W}_1} \underbrace{\begin{bmatrix} \Re(z_1) \\ \Im(z_1) \end{bmatrix}}_{\mathbf{s}_1}, \quad (11)$$

where

$$\mathbf{Q}_k = \begin{bmatrix} \Re(e^{2jk\pi/3}) & \Im(e^{2jk\pi/3}) \\ \Im(e^{2jk\pi/3}) & -\Re(e^{2jk\pi/3}) \end{bmatrix}. \quad (12)$$

Table I presents the expressions of  $\mathbf{W}_k$  and  $\mathbf{s}_k$  for the classes  $C_1$ ,  $C_2$ ,  $C_3$ , and  $C_4$ .

Note that the proposed classification is also related to the commonly used ABC classification [41]. The ABC classification is composed of nine sag/swell signatures, denoted with letters from A to I [23], [41]. These signatures are characterized by a complex pre-fault voltage,  $E$ , and a complex post-fault voltage,  $V$  [41]. For each

TABLE I  
EXPRESSIONS OF  $\mathbf{W}_k$  AND  $\mathbf{s}_k$  WITH RESPECT TO CLASS  $C_k$ .

Class	$C_1$	$C_2$	$C_3$	$C_4$
k	1	2	3	4
$\mathbf{W}_k$	$\begin{bmatrix} \mathbf{Q}_0 \\ \mathbf{Q}_1 \\ \mathbf{Q}_2 \end{bmatrix}$	$\begin{bmatrix} \mathbf{Q}_0 & \mathbf{Q}_0 \\ \mathbf{Q}_1 & \mathbf{Q}_2 \\ \mathbf{Q}_2 & \mathbf{Q}_1 \end{bmatrix}$	$\begin{bmatrix} \mathbf{Q}_0 & \mathbf{Q}_0 \\ \mathbf{Q}_0 & \mathbf{Q}_1 \\ \mathbf{Q}_0 & \mathbf{Q}_2 \end{bmatrix}$	$\begin{bmatrix} \mathbf{Q}_0 & \mathbf{Q}_0 & \mathbf{Q}_0 \\ \mathbf{Q}_0 & \mathbf{Q}_1 & \mathbf{Q}_2 \\ \mathbf{Q}_0 & \mathbf{Q}_2 & \mathbf{Q}_1 \end{bmatrix}$
$\mathbf{s}_k$	$\begin{bmatrix} \Re(z_1) \\ \Im(z_1) \end{bmatrix}$	$\begin{bmatrix} \Re(z_1) \\ \Im(z_1) \\ \Re(z_2) \\ \Im(z_2) \end{bmatrix}$	$\begin{bmatrix} \Re(z_0) \\ \Im(z_0) \\ \Re(z_1) \\ \Im(z_1) \end{bmatrix}$	$\begin{bmatrix} \Re(z_0) \\ \Im(z_0) \\ \Re(z_1) \\ \Im(z_1) \\ \Re(z_2) \\ \Im(z_2) \end{bmatrix}$

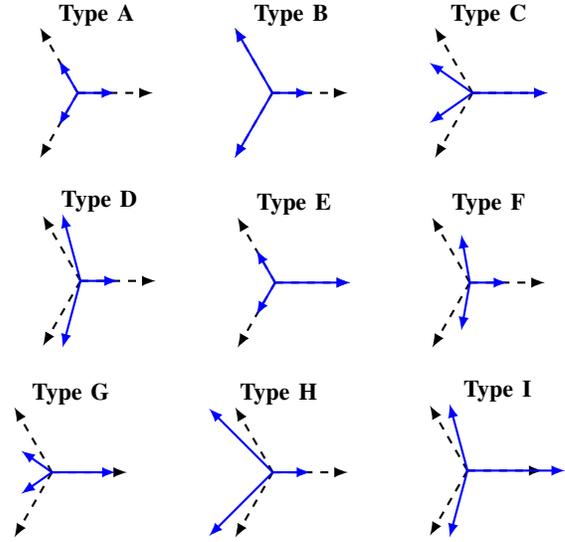


Fig. 1. ABC Classification: Sags and swells signatures [23].

TABLE II  
LINK BETWEEN THE PROPOSED AND ABC CLASSIFICATIONS.

Type	$z_0$	$z_1$	$z_2$	Class
Balanced	0	$E$	0	$C_1$
A	0	$V$	0	
C	0	$\frac{V+E}{2}$	$\frac{E-V}{2}$	
D	0	$\frac{V+E}{2}$	$\frac{V-E}{2}$	
F	0	$\frac{2V+E}{3}$	$\frac{V-E}{3}$	
G	0	$\frac{2V+E}{3}$	$\frac{E-V}{3}$	
H	$\frac{V-E}{3}$	$E$	0	
I	$\frac{3(E-V)}{2}$	$E$	0	
B	$\frac{V-E}{3}$	$\frac{V+2E}{3}$	$\frac{V-E}{3}$	
E	$\frac{E-V}{3}$	$\frac{2V+E}{3}$	$\frac{E-V}{3}$	

signature, the phasor configuration is illustrated in Fig. 1, where the dashed and solid arrows present the phasor configuration before and after voltage sag/swell, respectively. The link between the proposed and ABC classifications is presented in Table II. In particular, one can note that the proposed classification can be used to pre-classify the nine signatures of the ABC classification.

### C. General Vectorized Signal Model

This section presents the general vectorized signal model. Using (8) and (10), the signal model can be described under the general form

$$\mathbf{x} = \mathbf{M}_k \mathbf{s}_k + \mathbf{b}, \quad (13)$$

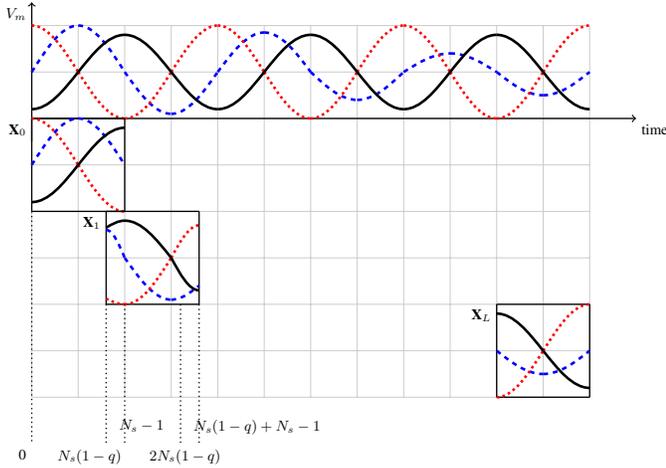


Fig. 2. Concept of sliding window under quasi-stationary conditions.

where  $k$  corresponds to the class number and

$$\mathbf{M}_k \triangleq (\mathbf{I}_3 \otimes \mathbf{A}) \mathbf{W}_k. \quad (14)$$

The goal of this paper is to determine the phasor configuration, i.e. the class number  $k$  and the signature, from the vectorized three-phase signal  $\mathbf{x}$ .

Note that, while the theoretical methods presented in the following sections are based on the stationary assumption, these methods can be easily extended to the non-stationary case. Indeed, when the signal parameters are time-varying, a straightforward solution is to use a short-time analysis as illustrated by Fig. 2. In Fig. 2, the analysis is performed on several signal blocks with a window length of  $N_s$  samples. By considering an overlapping parameter  $0 \leq q < 1$ , the  $l^{\text{th}}$  signal block can be mathematically expressed by

$$\mathbf{X}_l = \begin{bmatrix} x_0[N_b] & x_1[N_b] & x_2[N_b] \\ \vdots & \vdots & \vdots \\ x_0[N_e] & x_1[N_e] & x_2[N_e] \end{bmatrix}, \quad (15)$$

where  $N_b = lN_s(1-q)$ ,  $N_e = lN_s(1-q) + N_s - 1$ . In this context, the  $l^{\text{th}}$  vectorized block,  $\mathbf{x}_l = \text{vec}(\mathbf{X}_l)$ , is given by

$$\mathbf{x}_l = \mathbf{M}_k \mathbf{s}_{kl} + \mathbf{b}_l, \quad (16)$$

where  $\mathbf{s}_{kl}$  corresponds to the  $l^{\text{th}}$  augmented time-varying symmetrical components. By using a small window length  $N_s$ , the signal parameters and the class number  $k$  can be tracked over time.

### III. SIGNATURE CLASSIFIER

This section presents the proposed decision-tree classifier aiming at classifying the signal into one of the nine classes of the ABC classification. Specifically, the first subsection describes the proposed decision tree and the second one focuses on the decision algorithms.

#### A. Decision Tree

Fig. 3 depicts the decision tree of the proposed classifier. The proposed decision tree is based on two stages, which are the pre-classification into one of the 4 classes ( $\mathcal{C}_1$ ,  $\mathcal{C}_2$ ,  $\mathcal{C}_3$ , and  $\mathcal{C}_4$ ) and the final classification into one of the nine signatures of the ABC classification.

In the first stage, as the 4 classes are nested<sup>1</sup>, we propose to reformulate the classification problem as a pure *model order selection*

<sup>1</sup>For example, the class  $\mathcal{C}_1$  is a particular case of the class  $\mathcal{C}_3$

problem. Indeed, Table I shows that the pre-class can be determined from the identification of the model order, i.e. the size of the vector  $\mathbf{s}_k$ . Specifically, the size of the vector  $\mathbf{s}_k$  is equal to 2 for the class  $\mathcal{C}_1$ , 4 for the classes  $\mathcal{C}_2$  and  $\mathcal{C}_3$ , and 6 for the class  $\mathcal{C}_4$ . To determine the model order, we propose to use a detection technique based on Information Theoretic Criterion [43].

Once the nine signatures have been pre-classified into one of the 4 classes, the corresponding signature type can be classified by analyzing the symmetrical components. As these components are unknown, we propose to estimate them by using the Maximum Likelihood technique. Then, we determine the signature by analyzing the values of the estimated symmetrical components. Specifically, for  $\mathcal{C}_1$ , it is possible to discriminate between sag type A and balanced power system by comparing the value of  $|\hat{z}_1|$  with the pre-fault value. For  $\mathcal{C}_2$ , the value of  $|\hat{z}_1 + \hat{z}_2|$  allows the discrimination between type C and types D, F, and G. Then, the discrimination between type D and types F and G can be obtained by analyzing the value of  $|\hat{z}_1 - \hat{z}_2|$ . For class  $\mathcal{C}_3$ ,  $\Re e(\frac{\hat{z}_0}{\hat{z}_1})$  allows the classification between types I and H. Finally, for  $\mathcal{C}_4$ , the value  $|\hat{z}_1 - \hat{z}_0|$  allows the discrimination between types B and E. Note that the proposed decision tree is not able to discriminate between types F and G.

#### B. Proposed Decision Algorithms

In this subsection, we show how to pre-classify the signal into 4 classes using Information Theoretical Criteria, and how to estimate the symmetrical components  $z_1$ ,  $z_2$ , and  $z_3$  using the Maximum Likelihood technique.

Regarding the pre-classifier, the selected class  $\mathcal{C}_k$  based on Information Theoretical Criteria is the one that minimizes the following penalized likelihood function [44]

$$\hat{k} = \arg \min_{k=1,2,3,4} -2 \ln p(\mathbf{x}, \hat{\mathbf{s}}_k) + \gamma_k, \quad (17)$$

where  $\ln p(\mathbf{x}, \hat{\mathbf{s}}_k)$  denotes the log-likelihood function of the vectorized signal  $\mathbf{x}$  for the class  $k$ , and  $\hat{\mathbf{s}}_k$  corresponds to the Maximum Likelihood Estimator of  $\mathbf{s}_k$ . The term  $\gamma_k$  is a penalty function that depends on the total number of samples and on the number of free parameters. In the following paragraphs, we provide explicit expressions for the log-likelihood function and penalty term.

1) *Expression of the log-likelihood function*: Under the assumption that the additive noise is Gaussian distributed with a zero mean and a variance equal to  $\sigma^2$  i.e.  $\mathbf{b} \sim \mathcal{N}(\mathbf{0}, \sigma^2 \mathbf{I}_{3N})$ , it has been demonstrated in [43] that the log-likelihood function  $\ln p(\mathbf{x}, \hat{\mathbf{s}}_k)$  is equal to

$$-2 \ln p(\mathbf{x}, \hat{\mathbf{s}}_k) = \text{constant} + 3N \ln \hat{\sigma}_k^2, \quad (18)$$

where  $\hat{\sigma}_k^2$  is the Maximum Likelihood Estimator of the noise variance under the assumption that the signal comes from class  $\mathcal{C}_k$ . Note that, in addition to the model order, the estimator of the noise variance  $\hat{\sigma}^2$  also provides a simple measure of the goodness of fit for competing models with the same model order such as  $\mathcal{C}_2$  and  $\mathcal{C}_3$ . Mathematically, the noise variance estimator is given by

$$\hat{\sigma}_k^2 = \frac{1}{3N} \|\mathbf{x} - \mathbf{M}_k \hat{\mathbf{s}}_k\|^2, \quad (19)$$

where  $\hat{\mathbf{s}}_k$  corresponds to the Maximum Likelihood Estimator of the vector  $\mathbf{s}_k$ . As  $\hat{\mathbf{s}}_k = (\mathbf{M}_k^T \mathbf{M}_k)^{-1} \mathbf{M}_k^T \mathbf{x}$ , it follows that

$$\hat{\sigma}_k^2 = \mathbf{x}^T \mathbf{P}_k^\perp \mathbf{x}, \quad (20)$$

where  $\mathbf{P}_k^\perp$  is the orthogonal projector onto the null space of  $\mathbf{M}_k$ , which is defined as [45]

$$\mathbf{P}_k^\perp \triangleq \mathbf{I}_{3N} - \mathbf{M}_k (\mathbf{M}_k^T \mathbf{M}_k)^{-1} \mathbf{M}_k^T. \quad (21)$$

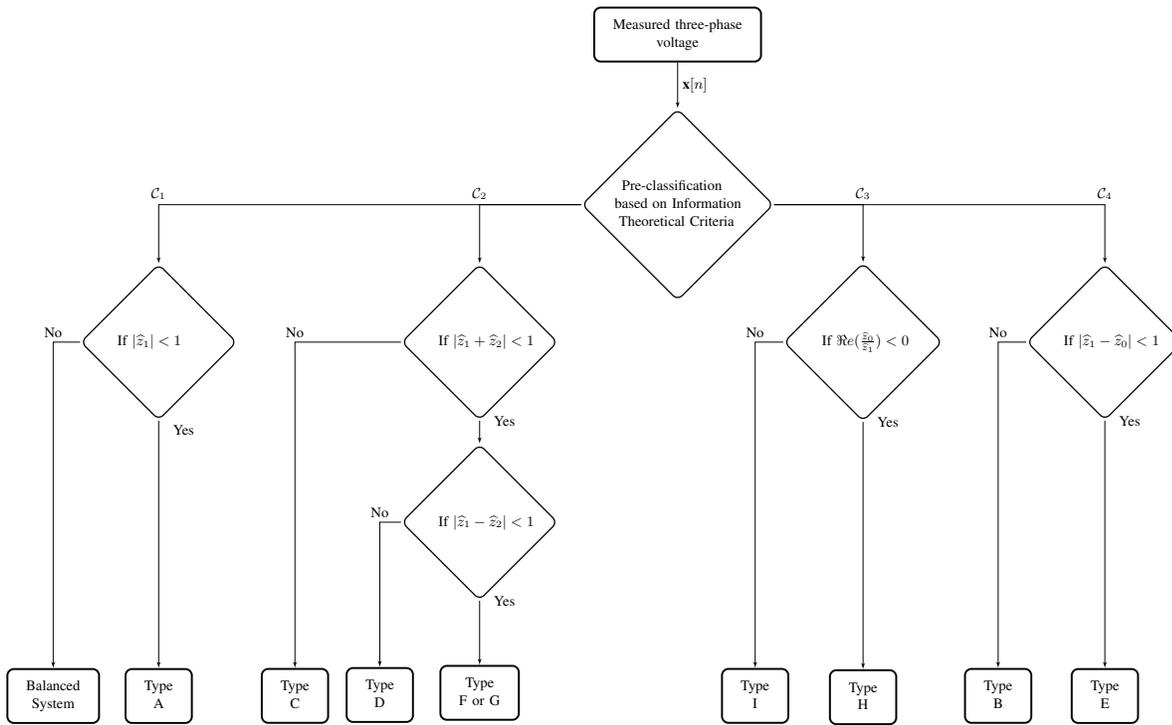


Fig. 3. Flowchart of the proposed classification algorithm.

It is worth mentioning that the inverse of  $\mathbf{M}_k^T \mathbf{M}_k$  is generally difficult to obtain analytically. Nevertheless, in some particular cases, this inverse has a simple closed form. Indeed, when the number of samples is large, i.e.  $N \gg 1$  or when  $N$  is a multiple of a half of the signal period, i.e.  $N = k\pi/\omega_0$ , it can be checked that  $\mathbf{A}^T \mathbf{A} = \frac{N}{2} \mathbf{I}$ . Furthermore, as  $\mathbf{W}_k^T \mathbf{W}_k = 3\mathbf{I}$ , it follows that  $\mathbf{M}_k^T \mathbf{M}_k \approx \frac{3N}{2} \mathbf{I}$ . Therefore, the orthogonal projector,  $\mathbf{P}_k^\perp$ , can be approximated by

$$\mathbf{P}_k^\perp \approx \mathbf{I}_{3N} - \frac{2}{3N} \mathbf{M}_k \mathbf{M}_k^T. \quad (22)$$

Based on the values of  $\mathbf{P}_k^\perp$ , we propose two different pre-classifiers: the Maximum Likelihood (ML) classifiers and the Approximate (App) one. The ML classifier is obtained by using the exact value of the orthogonal projector (21) in (20), (18), and (17). The App classifier is obtained by using the approximated projector (22) in (20), (18), and (17). Finally for the ML and App classifiers, the estimated classes are respectively given by

$$\hat{k}^{ML} = \arg \min_{k=1,2,3,4} 3N \ln(\mathbf{x}^T \mathbf{P}_k^\perp \mathbf{x}) + \gamma_k \quad (23)$$

$$\hat{k}^{App} = \arg \min_{k=1,2,3,4} 3N \ln\left(\|\mathbf{x}\|^2 - \frac{2}{3N} \|\mathbf{M}_k^T \mathbf{x}\|^2\right) + \gamma_k, \quad (24)$$

where  $\|\mathbf{x}\|^2 \triangleq \mathbf{x}^T \mathbf{x}$  corresponds to the squared norm of  $\mathbf{x}$ . Note that the App pre-classifier has a lower computational complexity than the ML pre-classifier since it requires a smaller number of matrix multiplications and does not involve any matrix inversion.

2) *Expression of  $\gamma_k$* : The goal of the penalty term  $\gamma_k$  is to promote simplicity over complexity. Mathematically, this function penalizes the log-likelihood function with respect to the number of samples,  $3N$ , and estimated parameters,  $n_k$ . Several penalty terms have been proposed in the literature based on different motivations [43]. In particular, the most commonly used penalty terms are the Akaike Information Criterion (AIC)  $\gamma_k^{AIC} = 2n_k$ , and the Bayesian Information Criterion (BIC)  $\gamma_k^{BIC} = n_k \ln(3N)$ . For the class  $k$ , the number of estimated parameters is equal to  $n_k = l_k + 1$ , where  $l_k$

 TABLE III  
 PENALTY FUNCTION WITH RESPECT TO CLASS  $\mathcal{C}_k$ .

Class	$\mathcal{C}_1$	$\mathcal{C}_2$	$\mathcal{C}_3$	$\mathcal{C}_4$
$n_k$	3	5	5	7
$\gamma_k^{AIC}$	6	10	10	14
$\gamma_k^{BIC}$	$3 \ln(3N)$	$5 \ln(3N)$	$5 \ln(3N)$	$7 \ln(3N)$

corresponds to the size of  $\hat{\mathbf{s}}_k$  and the number 1 is due to the noise variance estimation. Finally, the values of the AIC and BIC criteria are summed up in Table III for classes  $\mathcal{C}_1$ ,  $\mathcal{C}_2$ ,  $\mathcal{C}_3$ , and  $\mathcal{C}_4$ .

The second stage of the proposed classifier uses the symmetrical component estimates to determine the signature type. Statistically, the ML estimator of  $\hat{z}_0$ ,  $\hat{z}_1$ , and  $\hat{z}_2$  can be easily extracted from the ML estimator of  $\mathbf{s}_k$ . The exact and approximate estimators of  $\mathbf{s}_k$  are respectively given by [44]

$$\hat{\mathbf{s}}_k^{ML} = \left(\mathbf{M}_k^T \mathbf{M}_k\right)^{-1} \mathbf{M}_k^T \mathbf{x} \quad (25)$$

$$\hat{\mathbf{s}}_k^{App} = \frac{2}{3N} \mathbf{M}_k^T \mathbf{x}. \quad (26)$$

Then, the expression of the  $v^{th}$  symmetrical component, denoted  $\hat{z}_v$ , can be obtained from  $\hat{\mathbf{s}}_k^{ML}$ , or  $\hat{\mathbf{s}}_k^{App}$ , by constructing the complex value

$$\hat{z}_v = [\hat{\mathbf{s}}_k]_{2u} + j[\hat{\mathbf{s}}_k]_{2u+1}, \quad (27)$$

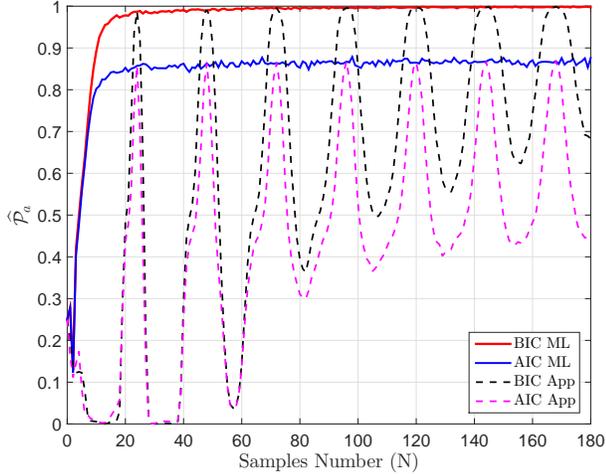
where  $[\hat{\mathbf{s}}_k]_u$  corresponds to the  $u^{th}$  element of  $\hat{\mathbf{s}}_k$ . Note that the index  $v$  depends on the class  $\mathcal{C}_k$ . Indeed using Table I, it can be readily checked that  $v = 1$  when  $u = 0$  for class  $\mathcal{C}_1$ ,  $v = u + 1$  for class  $\mathcal{C}_2$ ,  $v = u$  for classes  $\mathcal{C}_3$  and  $\mathcal{C}_4$ .

#### IV. SIMULATION AND EXPERIMENTAL RESULTS

In this section the performance of the proposed classifier illustrated in Fig. 3 is evaluated through synthetic signals and real power

TABLE IV  
 4-CLASSES: SIMULATION PARAMETERS.

	$C_1$	$C_2$	$C_3$	$C_4$
$c_0$	$0.5\angle -20^\circ$	$1\angle -20^\circ$	$0.5\angle -20^\circ$	$1\angle -20^\circ$
$c_1$	$0.5\angle -140^\circ$	$0.66\angle -159.10^\circ$	$1.32\angle -159.10^\circ$	$0.5\angle -140^\circ$
$c_2$	$0.5\angle 100^\circ$	$0.66\angle 119.11^\circ$	$1.32\angle 119.11^\circ$	$0.5\angle 100^\circ$


 Fig. 4. Average probability of correct classification versus samples number for  $SNR = 15$  dB.

system data. Two classifiers have been implemented: the Maximum Likelihood (ML) classifier composed of the exact ML pre-classifier in (23) and the ML estimator of  $\hat{z}_v$  in (25), and the approximate (App) classifier composed of the approximate pre-classifier in (24) and the approximate ML estimator of  $\hat{z}_v$  in (26).

#### A. Monte Carlo Simulation Results

In this subsection, the two pre-classifiers are evaluated using synthetic signals. The classification performance, which is quantified through the average probability of correct classification, is evaluated using both the AIC and BIC penalty terms. The average probability of correct classification is estimated using  $N_{mc} = 1000$  Monte Carlo trials for each class  $C_k$ . In each simulation, the signal is generated from the model defined in (1) with  $\omega_0 = 2\pi f_0/F_s$ , where  $f_0 = 50$  Hz and  $F_s = 48 \times f_0 = 2400$  Hz. The amplitudes and initial phases of the three complex phasors for 4-classes are given in Table IV. Then, the average probability of correct classification is estimated as follows

$$\hat{\mathcal{P}}_a = \frac{1}{4N_{mc}} \sum_{k=1}^4 \sum_{n=1}^{N_c} \delta(k - \hat{k}_n), \quad (28)$$

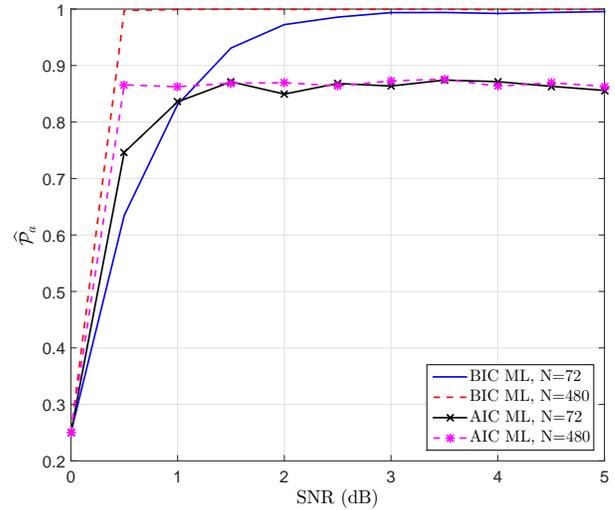
where  $\hat{k}_n$  is the estimated class for the  $n^{th}$  trial, and  $\delta(l)$  is the Kronecker delta which is equal to 1 if  $l = 1$  and zero elsewhere. In the next subsections, the average probability of correct classification is analyzed for different signal lengths,  $N$ , and Signal to Noise Ratio ( $SNR$ ), where the  $SNR$  is defined as

$$\eta = \frac{1}{6\sigma^2} \sum_{k=0}^2 a_k^2, \quad (29)$$

and  $\sigma^2$  corresponds to the noise variance.

##### 1) Probability of correct classification versus number of samples:

Fig. 4 shows the influence of the number of samples on the average probability of correct classification when the  $SNR$  is equal to 15 dB. It can be observed that the ML pre-classifier outperforms, in most of


 Fig. 5. Average probability of correct classification versus  $SNR$  for  $N = 72$  and  $N = 480$ .

the cases, the approximate one. Nevertheless, these two pre-classifiers lead to the same probability of correct classification when the number of samples is large or when  $N$  is a multiple of a half cycle i.e.  $N = (48/2)k = 24k$ . It is important to note that phasor measurement units (PMUs) can measure 50/60 Hz AC waveforms (voltages and currents) typically at a rate of a multiple of a cycle (48 samples per cycle).

Regarding the penalty factors, we observe that the pre-classifier using BIC penalty term outperforms the pre-classifier using AIC penalty term whatever the signal length is, for the ML and App pre-classifiers. In particular, we can note that for large  $N$  the BIC penalty term leads to an average probability of correct classification equal to 1, while the AIC penalty term leads to a smaller average probability. For small  $N$ , we also note that the BIC has a faster response time than the AIC penalty term.

##### 2) Probability of correct classification versus noise variance:

Fig. 5 highlights the influence of the  $SNR$  on the average probability of correct classification ( $\hat{\mathcal{P}}_a$ ). In this simulation, the number of samples  $N$  is set to 72 and 480 samples (multiple of a half-cycle). Under these conditions, the ML and approximate pre-classifiers lead to the same probability of correct classification. For  $N = 72$  samples, the BIC ML pre-classifier leads to  $\hat{\mathcal{P}}_a = 1$  when the  $SNR$  is greater than 3 dB. For  $N = 480$  samples, the BIC ML pre-classifier leads to  $\hat{\mathcal{P}}_a = 1$  when  $SNR$  is greater than 0.5 dB. This clearly shows that the proposed pre-classifier has good capabilities under a highly noisy environment. For the AIC pre-classifier, we observe that  $\hat{\mathcal{P}}_a$  is not equal to 1 even for large  $SNRs$  and  $N$ . To explain this limitation, Tables V and VI present the confusion matrices when  $N = 480$  samples and at  $SNR = 5$  dB. For the ML pre-classifier using BIC penalty term, we observe that each trial is correctly classified since the confusion matrix only contains diagonal elements. For the ML pre-classifier using the AIC penalty term, we observe that the confusion matrix also contains non-diagonal elements and is upper triangular. The upper triangular structure shows that the AIC penalty term seems to overestimate the model order.

##### 3) Robustness of the proposed classifier:

This subsection evaluates the performance of the proposed algorithm under harmonic environments. By introducing harmonic components in (1), the signal model

TABLE V  
AIC CRITERION: ML PRE-CLASSIFIER CONFUSION MATRIX.

	$\mathcal{C}_1$	$\mathcal{C}_2$	$\mathcal{C}_3$	$\mathcal{C}_4$
$\mathcal{C}_1$	741	135	124	0
$\mathcal{C}_2$	0	874	0	126
$\mathcal{C}_3$	0	0	861	147
$\mathcal{C}_4$	0	0	0	1000

TABLE VI  
BIC CRITERION: ML PRE-CLASSIFIER CONFUSION MATRIX.

	$\mathcal{C}_1$	$\mathcal{C}_2$	$\mathcal{C}_3$	$\mathcal{C}_4$
$\mathcal{C}_1$	999	0	1	0
$\mathcal{C}_2$	0	1000	0	0
$\mathcal{C}_3$	0	0	1000	0
$\mathcal{C}_4$	0	0	0	1000

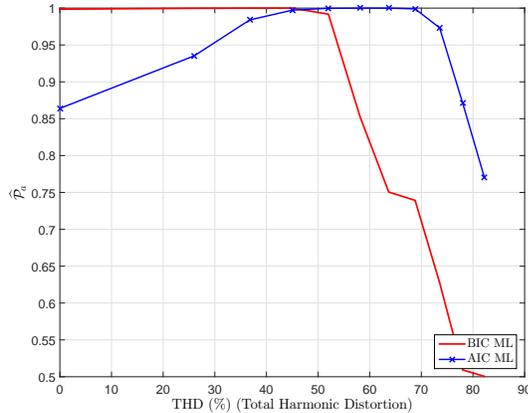


Fig. 6. Harmonic effect on the proposed classifier. Comparison between ML classifiers using BIC and AIC penalty terms.

can be described by

$$x_m[n] = a_m \cos(n\omega_0 + \phi_m) + \sum_{h=3,5,7,\dots} \alpha (a_{mh} \cos(hn\omega_0 + \phi_{mh})) + b_m[n], \quad (30)$$

where  $a_{mh}$  and  $\phi_{mh}$  correspond to the amplitude and initial phase of the  $h^{\text{th}}$  order harmonic, respectively. The quantity  $\alpha > 0$  corresponds to the harmonic parameter. The harmonic amplitudes are set to  $a_{m5} = 0.06$  pu,  $a_{m7} = 0.05$  pu,  $a_{m11} = 0.015$  pu,  $a_{m13} = 0.03$  pu, and  $a_{m13} = 0.03$  pu.

Fig. 6 shows the  $\hat{P}_a$  of the proposed pre-classifiers versus the Total Harmonic Distortion (THD) for  $N = 144$  samples and  $SNR = 5$  dB. The Total Harmonic Distortion is controlled by varying the different harmonics amplitudes through the scalar  $\alpha$ . We show that the performances of the proposed pre-classifiers decreases for a high value of THD. Furthermore, we observe that for a THD less than 50% the BIC ML pre-classifier leads to a constant  $\hat{P}_a = 1$ , while for the AIC pre-classifier it is increasing with respect to the THD. For a THD  $> 70\%$ , the  $\hat{P}_a$  of both pre-classifiers is decreasing when the THD increases due to the model mismatch.

4) *Computation complexity*: Fig. 7 compares the computation complexity (in seconds) between the ML and App classifiers. The computation time are evaluated by averaging the execution time through 1000 Monte Carlo trials. Results show that both classifiers computation times increase proportionally to the number of samples

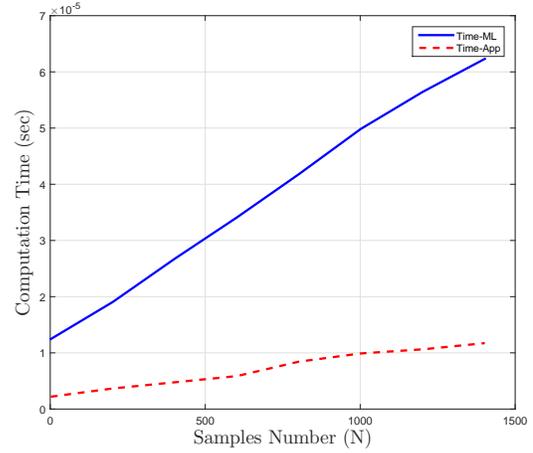


Fig. 7. Computation time versus  $N$ : Comparison between ML and Approximate classifiers.

TABLE VII  
VOLTAGE SAGS TYPE C: COMPARISON OF THE PROPOSED CLASSIFIER WITH SC AND TP-TA ALGORITHMS

Case	<b>C</b>	<b>C</b>	<b>C</b>
$\hat{V}_a$	$0.85 \angle -20^\circ$	$0.85 \angle -20^\circ$	$0.85 \angle -20^\circ$
$\hat{V}_b$	$0.56 \angle -118^\circ$	$0.46 \angle -110^\circ$	$0.65 \angle -168^\circ$
$\hat{V}_c$	$0.56 \angle 160^\circ$	$0.65 \angle 168^\circ$	$0.46 \angle 110^\circ$
<b>SCA</b>	<b>D<sub>c</sub></b>	<b>D<sub>c</sub></b>	<b>C<sub>a</sub></b>
<b>TP-TAA</b>	<b>C<sub>a</sub></b>	<b>C<sub>a</sub></b>	<b>D<sub>c</sub></b>
<b>BIC ML</b>	<b>C</b>	<b>C</b>	<b>C</b>

$N$ , while having different slopes. Specifically, the slope of the App classifier is lower than the ML classifier one. Therefore, when the signal length  $N$  is a multiple of a half-cycle, the approximate classifier is an attractive choice for pre-classification since it has a lower computational cost and reaches the statistical performance of the ML classifier.

5) *Classification comparison*: This subsection proposes a comparison of the ML classifier using the BIC penalty term (BIC-ML) with two others techniques, namely the symmetrical components and the three-phase three-angle algorithms (SCA and TP-TAA, respectively). The SCA and TP-TAA allow identifying the six voltage sags types among the C and D types. For the SC algorithm, the angle between the drop in positive- and negative-sequence voltages is used for classification [18]. The TP-TA algorithm is based on the remains rms voltage (RV), the inverse remains voltage (IRV), the delta inverse remains voltage ( $\Delta$ IRV), and the three angles  $\alpha$ ,  $\beta$ , and  $\gamma$  [21]. In the following, the performances of the classification algorithms are evaluated using the phasor configurations presented in [21]. For each technique, the phasors are estimated using the ML estimator in (25) with a half-cycle window length.

From Tables VII, VIII, IX, and X, we observe that the proposed classifier (BIC-ML) leads to an accurate classification of voltage sags in all cases, while the SC and TP-TA algorithms exhibit erroneous classification under large-phase angle jump and amplitude. These results show that the proposed algorithm has higher classification performance than the SC and TP-TA algorithms.

## B. Experimental Tests

In this subsection, the performances of the ML classifiers using BIC and AIC penalty terms are evaluated using real power system

TABLE VIII

VOLTAGE SAGS TYPE C: COMPARISON OF THE PROPOSED CLASSIFIER WITH SC AND TP-TA ALGORITHMS

Case	<b>C</b>	<b>C</b>	<b>C</b>
$\hat{V}_a$	$0.85\angle -20^\circ$	$0.85\angle -20^\circ$	$0.92\angle 0^\circ$
$\hat{V}_b$	$0.78\angle -177^\circ$	$0.65\angle -168^\circ$	$0.80\angle -122^\circ$
$\hat{V}_c$	$0.34\angle 104^\circ$	$0.46\angle 110^\circ$	$0.80\angle 123^\circ$
<b>SCA</b>	<b>C<sub>a</sub></b>	<b>D<sub>c</sub></b>	<b>C<sub>a</sub></b>
<b>TP-TAA</b>	<b>C<sub>a</sub></b>	<b>C<sub>a</sub></b>	<b>C<sub>a</sub></b>
<b>BIC ML</b>	<b>C</b>	<b>C</b>	<b>C</b>

TABLE IX

VOLTAGE SAGS TYPE D: COMPARISON OF THE PROPOSED CLASSIFIER WITH SC AND TP-TA ALGORITHMS

Case	<b>D</b>	<b>D</b>	<b>D</b>
$\hat{V}_a$	$0.87\angle -20^\circ$	$0.10\angle 84.29^\circ$	$0.70\angle 0^\circ$
$\hat{V}_b$	$0.40\angle -131^\circ$	$0.81\angle -90.71^\circ$	$0.92\angle -114^\circ$
$\hat{V}_c$	$0.82\angle 133^\circ$	$0.91\angle 90.63^\circ$	$0.92\angle 110^\circ$
<b>SCA</b>	<b>D<sub>b</sub></b>	<b>D<sub>a</sub></b>	<b>D<sub>a</sub></b>
<b>TP-TAA</b>	<b>D<sub>b</sub></b>	<b>D<sub>a</sub></b>	<b>C<sub>b</sub></b>
<b>BIC ML</b>	<b>D</b>	<b>D</b>	<b>D</b>

TABLE X

VOLTAGE SAGS TYPE C AND D: COMPARISON OF THE PROPOSED CLASSIFIER WITH SC AND TP-TA ALGORITHMS

Case	<b>C</b>	<b>D</b>	<b>D</b>
$\hat{V}_a$	$1\angle 0.6^\circ$	$0.92\angle 06^\circ$	$0.70\angle 0^\circ$
$\hat{V}_b$	$0.81\angle -152^\circ$	$0.92\angle -130^\circ$	$0.92\angle -114^\circ$
$\hat{V}_c$	$0.47\angle 126^\circ$	$0.70\angle 120^\circ$	$0.92\angle 110^\circ$
<b>SCA</b>	<b>C<sub>a</sub></b>	<b>D<sub>c</sub></b>	<b>D<sub>a</sub></b>
<b>TP-TAA</b>	<b>C<sub>a</sub></b>	<b>C<sub>a</sub></b>	<b>C<sub>b</sub></b>
<b>BIC ML</b>	<b>C</b>	<b>D</b>	<b>D</b>

data obtained from the DOE/EPRI National Database of Power System Events [46]. The disturbances used in this subsection correspond to the events 2825, 2827, 2802, 2786, and 2911. These disturbance events correspond to different voltage sag and swell configurations. Regarding the classifier settings, the window length was set to a half-cycle (64 samples) with a half-cycle overlap. Figs. 8-12 present the three-phase signal, the amplitude of the estimated phasors, the selected pre-class and the estimated signature for the 5 events.

For event 1 (Fig. 8), we observe that both pre-classifiers using the BIC and the AIC penalty terms achieve the same results. Indeed, both pre-classifiers lead to null zero- and negative-sequences ( $C_1$ ) under balanced conditions. Under transient conditions a non-null symmetrical sequence is obtained ( $C_4$ ). It seems that both pre-classifiers can achieve a good classification under balanced or transient conditions. For event 2 (Fig. 9), both pre-classifiers achieve the same results under balanced conditions since they lead to null zero- and negative-sequences ( $C_1$ ). Under transient conditions, these pre-classifiers give different classification results. The BIC pre-classifier leads to a null zero-sequence ( $C_2$ ), while the AIC pre-classifier leads to a non-null symmetrical-sequence ( $C_4$ ). It is observed that after 0.12 s, the ML classifier using the AIC penalty term seems to give incorrect classification since it leads to a type FG instead of type A. In contrast, the ML classifier using the BIC penalty term seems to achieve good classification results. For event 3 (Fig. 10), we observe that both pre-classifiers achieve different classification results. Under balanced conditions, the pre-classifier using the BIC penalty term leads to null zero- and negative-sequences ( $C_1$ ), whereas the pre-

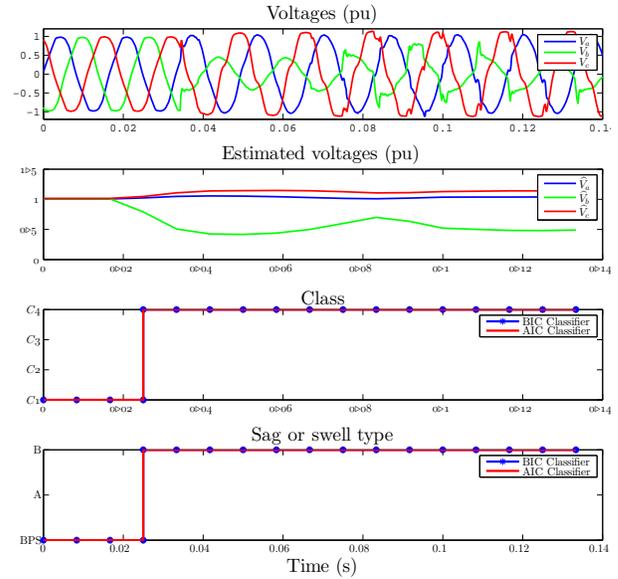


Fig. 8. Event 1 (2827): Voltage sag and swell classification. Comparison between ML classifiers using BIC and AIC penalty terms.

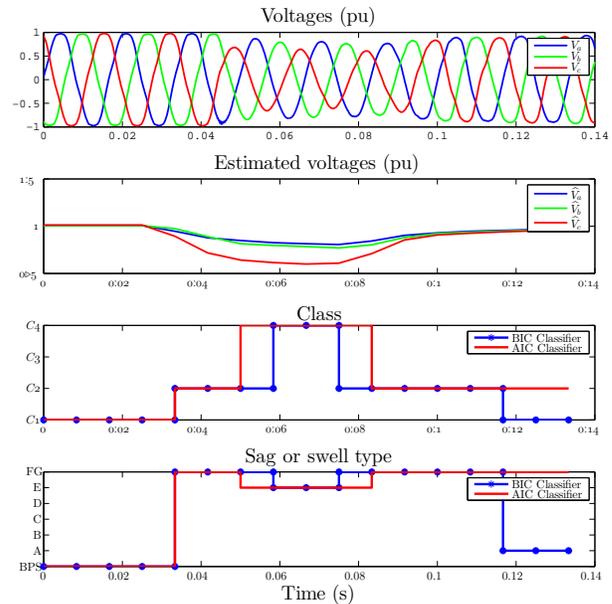


Fig. 9. Event 2 (2825): Voltage sag and swell classification. Comparison between ML classifiers using BIC and AIC penalty terms.

classifier using the AIC penalty term leads to a null zero-sequence ( $C_2$ ). Under transient conditions, the BIC pre-classifier leads to a null zero-sequence ( $C_2$ ) and the AIC pre-classifier leads to non-null symmetrical-sequences ( $C_4$ ). We can note that after 0.10 s both pre-classifiers lead to the same result. For event 4 (Fig. 11) both pre-classifiers lead to different results under balanced conditions ( $C_1$  and  $C_3$ ) but achieve the same result after 0.03 s. For event 5 (Fig. 12), the two pre-classifiers lead to the same results except between 0.03 s and 0.04 s. In most of the cases, we observe that the BIC classifier seems to achieve better classification results under balanced and transient conditions than the AIC classifier.

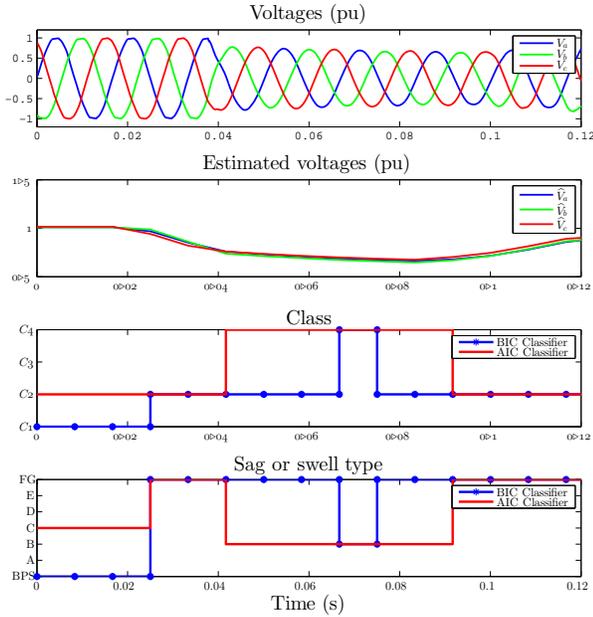


Fig. 10. Event 3 (2802): Voltage sag and swell classification. Comparison between ML classifiers using BIC and AIC penalty terms.

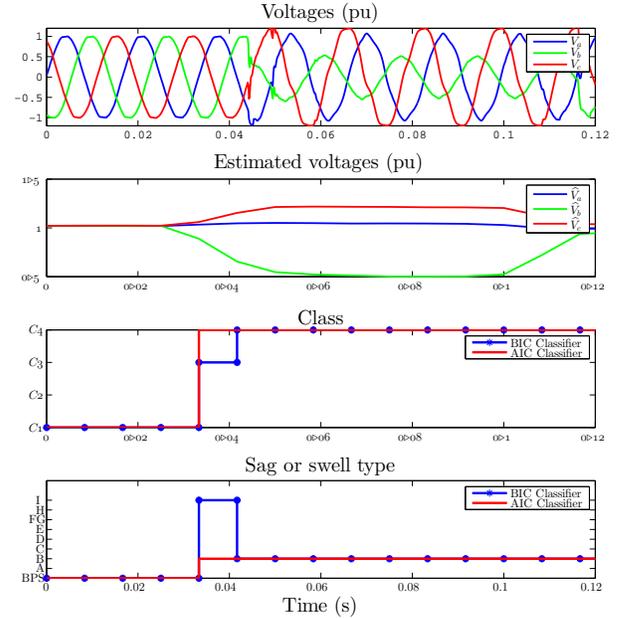


Fig. 12. Event 5 (2911): Voltage sag and swell classification. Comparison between ML classifiers using BIC and AIC penalty terms.

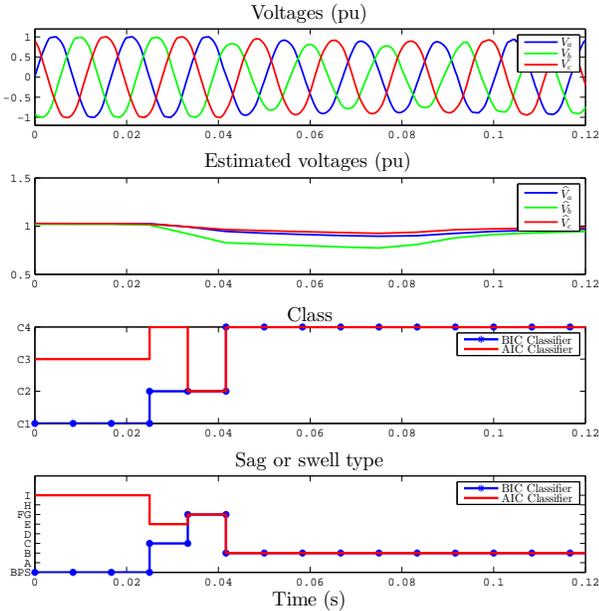


Fig. 11. Event 4 (2786): Voltage sag and swell classification. Comparison between ML classifiers using BIC and AIC penalty terms.

### C. Discussion

The previous sections have focused on the influence of signal length, noise level, harmonics, and window length (overlap) on the performance of the proposed classifiers (ML and approximate classifiers with BIC and AIC penalty terms). Simulation results have clearly shown that the ML classifier using the BIC penalty term achieves higher classification performances whatever the number of samples and  $SNR$  are.

The statistical performances of the ML and App classifiers depend on the number of samples,  $N$ , and on the  $SNR$ . Specifically, increasing the value of  $N$  or  $SNR$  also increases the classification performance of the ML classifier. Regarding the differences between the ML and

App classifiers, simulation results have shown that the ML classifier generally leads to the best classification performance. However, it should be mentioned that the approximate classifier can reach the performance of the ML classifier for particular cases, especially when the signal length  $N$  is a multiple of a half-cycle. Concerning the penalty term, most simulations have shown that the classifier using the BIC penalty term outperforms the AIC-based classifier. Indeed, simulation results have shown that the AIC penalty term seems to overestimate the number of non-zero symmetrical components.

Regarding the computation complexity, the approximate classifier has a lower computation time than the ML one. Indeed, this latter classifier involves larger number of matrix multiplications in comparison to the ML classifier. Nevertheless, the performance of the approximate classifier critically depends on the number of samples. Specifically, the classifier performance rapidly degrades when the number of samples is not a multiple of a half-cycle.

Under quasi-stationary conditions, i.e. when the signal parameters are time-varying, the tracking of the signal class requires a small sample window length,  $N$ . Nevertheless, there is a natural tradeoff between the tracking and statistical performance. According to Monte Carlo simulation, for the approximate classifier, we advise to select a window length  $N$  equal to a multiple of a half-cycle. In particular, to meet the minimum sag and swell durations defined in the standard IEEE std. 1159, we recommend to choose a window length equal to a half-cycle. To easily meet this criterion, we also advise to choose a sampling frequency equal to  $F_s = N f_0$  where  $N \gg 2$  and  $f_0$  is the signal frequency ( $f_0 = 50$  Hz or  $f_0 = 60$  Hz).

## V. CONCLUSION

This paper dealt with power quality disturbances classification in three-phase unbalanced power systems with a particular focus on voltage sags and swells. A new classification approach based on Information Theoretical Criteria has been proposed. This approach is mainly based on two steps: 1) the signal pre-classification into one of 4 pre-classes, where each class contains one or various sags or swells types and depends on the number of non-zero symmetri-

cal components, 2) the signature type classification using the ML estimate of the symmetrical components.

Regarding the proposed classifier, we have investigated the use of two Information Theoretical Criteria, namely the AIC and BIC. Simulation results have shown that the BIC criteria outperforms the AIC criteria in terms of average probability of correct classification for different data length and signal to noise ratio, whatever the classifier is. In particular, the analysis of the confusion matrices has indicated that the AIC seems to slightly overestimate the number of non-zero symmetrical component even for a large number of samples or signal to noise ratio. The results have also shown that the BIC classifier is robust against harmonic environment for moderate Total Harmonic Distortion (THD < 50%).

For applications requiring a low computational complexity, we have also proposed an approximate classifier that involves fewer matrix multiplications and no matrix inversion. Simulations based on synthetic signals and real power systems data have clearly shown that, in most of the cases, the exact classifier exhibits better statistical performances than the approximate one. However, simulation results have also shown that the approximate classifier has a much lower computation complexity and can lead to near optimal performances when  $N$  is a multiple of a half-cycle. Future investigations should deal with the evaluation of the proposed algorithms performances for the classification of other critical PQ disturbances.

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