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1	A new predictive dynamic model describing the effect of
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4	
5	H. Ben Yaghlene ^{a,b*} , I. Leguerinel ^a , M. Hamdi ^b , P. Mafart ^a
6	^a : Université Européenne de Bretagne, EA3882, Laboratoire Universitaire de Biodiversité et Ecologie
7	Microbienne, IFR148 ScInBioS, Université de Bretagne Occidentale, 6 rue de l'université, F29334 Quimper,
8	Cedex, France
9	^b : Laboratoire d'Ecologie et de Technologie Microbienne, Institut National des Sciences Appliquées et de
10	Technologie (INSAT), 2 Boulevard de la terre, B.P. 676, 1080 Tunis, Tunisie
11	
12	[*] Corresponding author: LUBEM, UBO, 6 rue de l'Université, F29334, Quimper Cedex, France. Tel.: +33 2 98
13	90 02 27; Fax: +33 2 98 90 85 44
14	E mail address: <u>hana.benyaghlene@univ-brest.fr</u>

16 Abstract

In this study, predictive microbiology and food engineering were combined in order to develop a new analytical model predicting the bacterial growth under dynamic temperature conditions. The proposed model associates a simplified primary bacterial growth model without lag, the secondary Ratkowsky "square root" model and a simplified two-parameter heat transfer model regarding an infinite slab. The model takes into consideration the product thickness, its thermal properties, the ambient air temperature, the convective heat transfer coefficient and the growth parameters of the micro organism of concern. For the validation of the overall model, five different combinations of ambient air temperature (ranging from 8 °C to 12 °C), product thickness (ranging from 1 cm to 6 cm) and convective heat transfer coefficient (ranging from 8 W/(m².K) to 60 W/(m².K)) were tested during a cooling

27 procedure. Moreover, three different ambient air temperature scenarios assuming alternated 28 cooling and heating stages, drawn from real refrigerated food processes, were tested. General 29 agreement between predicted and observed bacterial growth was obtained and less than 5% of 30 the experimental data fell outside the 95 percent confidence bands estimated by the bootstrap 31 percentile method, at all the tested conditions. Accordingly, the overall model was 32 successfully validated for isothermal and dynamic refrigeration cycles allowing for 33 temperature dynamic changes at the centre and at the surface of the product. The major 34 impact of the convective heat transfer coefficient and the product thickness on bacterial 35 growth during the product cooling was demonstrated. For instance, the time needed for the 36 same level of bacterial growth to be reached at the product's half thickness was estimated to 37 be 5 and 16.5 h at low and high convection level, respectively. Moreover, simulation results 38 demonstrated that the predicted bacterial growth at the air ambient temperature cannot be 39 assumed to be equivalent to the bacterial growth occurring at the product's surface or centre 40 when convection heat transfer is taken into account. Our results indicate that combining food 41 engineering and predictive microbiology models is an interesting approach providing very 42 useful tools for food safety and process optimisation.

43

44 Key words:

45

5 Predictive microbiology; Heat transfer; Dynamic models; Bacterial growth; Cooling; Heating.

46 Nomenclature

Α	Transfer area (m ²)
Bi	Biot number
Ε	Product thickness (m)
f'	Thermal proliferation value
Fo	Fourier number
h	Convective heat transfer coefficient $(W/(m^2.K))$
j	Lag factor for reduced temperature profile
k	Slope of the linear portion of the semi-logarithmic plot of reduced temperature vs time.
l	Characteristic dimension (m)
Ν	Microbial cell density at time t (CFU/mL)
N_0	Initial microbial cell density (CFU/mL)
0	Observed microbial cell density (log ₁₀ CFU/mL)
OD	Microbial optical density at time t
OD_0	Initial microbial optical density
Р	Predicted microbial cell density (log ₁₀ CFU/mL)
t	Time (s)
Т	Temperature of the product (°C)
T_{eq}	Equivalent temperature
T_{min}	Temperature below which no microbial growth occurs (°C)
T_{opt}	Temperature at which the microbial growth is optimal (°C)
T_0	Initial product temperature (°C)
T_{∞}	Ambient temperature (°C)
x	Distance from the centre (m)
x_{max}	Half-thickness for an infinite slab (m)
α	Thermal diffusivity of the product (m^2/s)
Г	Overall gamma function
γ	Thermal gamma function
λ	Thermal conductivity of the product (W/(m.K))
μ	Specific microbial growth rate (h ⁻¹)
μ_{opt}	Optimal specific microbial growth rate (h ⁻¹)
φ	First root of $\cot \varphi = \varphi / Bi$
φ_n	Roots of $\cot \varphi = \varphi / Bi$

49 **1. Introduction**

50 Predictive food microbiology involves knowledge of microbial growth responses to 51 environmental factors expressed in quantitative terms by mathematical equations (models) 52 (McMeekin et al., 1997). It is generally agreed that the most important environmental factor 53 that affects bacterial growth in food is temperature. This factor is constantly changing during 54 processing, storage and distribution of food products (Fujikawa et al., 2004). At the same 55 time, control organizations propose stringent requirements regarding monitoring of the 56 internal temperature of products being processed. For instance, according to the United States Department of Agriculture, the allowable growth of Clostridium perfringens during the 57 58 cooling of certain meat and poultry products should be limited to 1 log (U.S.D.A, 1999). In 59 the case of cured products, the guidelines recommend that products' internal temperature should be reduced from 54.4 °C to 26.6 °C in less than 5 h, and from 26.6 °C to 7.2 °C in the 60 61 next 10 h (15 h total cooling time).

62 Predictive microbiology is a useful tool for assessing and controlling food safety particularly 63 when models are able to cope with dynamic conditions such as changing temperatures. 64 Numerous published models, reported in Table 1, have dealt with the prediction of bacterial growth under dynamic temperature conditions. Generally, these works were based on 65 predictive models corresponding to isothermal bacterial growths which were modified in 66 67 order to consider the effect of temperature changes. These studies primarily aimed at 68 assessing the feasibility of predicting the bacterial growth at changing temperature. Indeed, 69 predicting bacterial growth under dynamic conditions has been shown to be possible via the 70 dynamic transformation of existing static models. According to the authors of the cited studies 71 (Table 1), the models' predictions agreed well with experimental results after temperature 72 changes.

73 Nevertheless, the considered scenarios of changing temperatures within bacterial models were 74 various. In some cases, typical temperature profiles were considered either by the use of 75 hypothetical ones or by the adoption of real temperature scenarios recorded while the studied 76 products had been processed. In other cases, temperature profiles were simulated from heat 77 transfer models. Mathematical models that integrate effectively heat transfer phenomena and 78 dynamic bacterial growth relationships are scarce (Amezquita et al., 2005; de Jong et al., 79 2005; Zwietering and Hasting, 1997). Armitage (1997) derived the temperature histories for 80 the deep leg and leg surface of a lamb carcass by using finite element models for dealing with 81 regular shapes. Temperature function integration technique (TFI) was applied to the 82 calculated temperature histories of five different cooling processes to simulate Escherichia 83 *coli* growth on the leg surface of each carcass during aging. TFI technique was previously introduced by Gill and Harrison (1985). Data related to the growth of six strains of E. coli 84 85 isolated from commercially packed livers were fitted according to the Ratkowsky model 86 (Ratkowsky et al., 1982) linking the growth rate to temperature. Total growth was obtained by 87 summation of partial growth calculated within sequential 3.75-min periods from the growth 88 rate for the average temperature within each period. Estimated bacterial growth during offals 89 cooling (cooling profiles were directly recorded on several offals being chilled) agreed well 90 with observed data with E. coli. Bellara et al. (2000) experimentally validated bacterial 91 growth modelling involving a heat transfer model of temperature fluctuations within a solid 92 object. From data related to E. coli W3110 growth in agar, a model was set up describing 93 bacterial growth as a function of temperature. This was then used in conjunction with a finite 94 difference heat transfer model describing temperature change in a cylinder in order to 95 calculate the bacterial growth that occurs in agar gel inside a cylindrical glass vessel under 96 conduction cooling. Excellent agreement was found between model simulations and experimental data. Alavi et al. (2001) determined the growth characteristics of Listeria 97

98 *monocytogenes* in sterilized whole milk. The parameter values of the Baranyi dynamic growth 99 model (Baranyi et al., 1995) were determined. Finite element software, ANSYS, was 100 implemented to determine temperature distributions in milk cartons subject to a time-varying 101 ambient temperature profile. The space-time-temperature data were input to the Baranyi 102 dynamic growth model, to predict the microbial population density distribution and the 103 average population density in the milk carton. Amezquita et al. (2005) developed a computer 104 simulation scheme to analyze heat transfer phenomena and temperature-dependent C. 105 perfringens growth during cooling of cooked boneless cured ham. The temperature history of ham was predicted from a finite element heat diffusion model. For C. perfringens growth, a 106 107 dynamic model was developed from the Baranyi's nonautonomous differential equation 108 (Baranyi and Roberts, 1994). The bacterium's growth model was integrated into the computer 109 program taking predicted temperature histories as input values. Validation of the model 110 predictions considered three different time-temperature cooling histories from 54.4 °C to 7.2 111 °C of the geometrical centre of a large cooked boneless ham. In a further work (Corradini et 112 al., 2006), the same data were fitted with the ad hoc empirical models in order to define the 113 three parameters temperature dependence of the modified version of the logistic primary 114 model. The continuous rate equation was solved incrementally by a numerical procedure 115 implemented in general purpose software. In both Amezquita et al. (2005) and Corradini et al. 116 (2006) works, predicted C. perfringens growth curves obtained from dynamic modelling 117 showed good agreement with observed results for the tested cooling scenarios. The integrated 118 modelling approach for predicting microbial behaviour during processing was reviewed by 119 Lebert and Lebert (2006).

120 Combination of predictive microbiology and food engineering allows both the assessment of a 121 process in relation to risk and its optimisation (Mafart, 2005). In spite of all the advances 122 made in modelling microbial growth, proposing and improving new overall models which 123 combine predictive microbiology and heat transfer phenomena is an obvious necessity. The 124 more simple the proposed models and the more realistic the considered conditions are, the 125 easiest is their implementation to food processes.

126 In the present study, we aimed to develop a new analytical model combining bacterial growth 127 prediction and food engineering. Our goal was for the overall model to be simple and robust, 128 with minimum involved parameters, and to integrate the process conditions. The proposed 129 model is the association of three equations: a simplified primary model consisting of a simple 130 exponential growth equation without lag time, the Ratkowsky "square root" model linking the 131 specific growth rate to temperature (Ratkowsky et al., 1982), and a simplified two-parameter 132 heat transfer model regarding an infinite slab. While classical models assume that ambient 133 temperature is immediately reached at the growth medium, this work takes into account, not 134 only the air temperature, but also the thickness of the medium, its thermal properties and the convective heat transfer coefficient. In addition, the proposed model may be easily 135 implemented to various micro organisms having known growth parameters. 136

137 **2. Development of the model**

138 **2.1. Heat transfer modelling**

139 All cooling processes for solid materials exhibit similar behaviour. After an initial 'lag', the 140 reduced temperature at the thermal centre of the food item decreases exponentially. The linear 141 portion of the cooling curve (obtained by plotting, on semi-logarithmic axes, the reduced temperature $(T_{\infty} - T)/(T_{\infty} - T_0)$ versus time (Becker and Fricke, 2004), see Fig. A1 in the 142 appendix) can typically be described by the simplified linear asymptotic form of the general 143 heat transfer model, valid for Fourier number $Fo \ge 0.2$ with $Fo = \alpha \cdot t/l^2$ where α is thermal 144 145 diffusivity of the product, l is the characteristic dimension of the product, T is the local temperature of the product at the time t, T_0 is the initial temperature of the product, T_{∞} is the 146

147 cooling medium temperature (pulsed air). Consequently, the heating or cooling kinetic is148 expressed as follows:

149
$$T = T_{\infty} \left(1 - j e^{-kt} \right) + T_0 j e^{-kt}$$
(1)

150 Where *j* is the lag factor and *k* is the slope of the linear portion of the semi-logarithmic plot of 151 reduced temperature *vs* time. The value of the parameter *k* depends upon the product shape, *l*, 152 α and the Biot number $Bi = hl/\lambda$, where *h* is the convective heat transfer coefficient between 153 the product surface area and the ambient air and λ is the thermal conductivity of the product. 154 A low Biot number (Bi < 0.1) indicates that the internal resistance to heat transfer is 155 negligible, and thus, the temperature within the object is uniform at any given instant in time 156 while the external thermal resistance can be neglected for Bi > 40 (Mafart, 1997).

157 The governing differential equation for infinite slab is given as follows with the initial 158 (uniform distribution of temperature) and boundary condition (surface convection):

159
$$\frac{\partial T}{\partial t} = \alpha \frac{\partial^2 T}{\partial x^2}$$
(2)

160 where *x* is distance from the centre. For initial condition of uniform temperature and boundary 161 conditions of central symmetry and convective heat transfer at the surface, solution for Eq. (2) 162 is supplied by the infinite series given by Carslaw and Jaeger (1986) (see Eq. (20) in the 163 appendix). It is a general knowledge that use of the first term of this series would be enough 164 when the Fourier number is greater than 0.2 since the temperature change after that certain time would be linear (Becker and Fricke, 2004; Bimbenet et al., 2002; Caro-Corrales et al., 165 166 2002; Dincer, 1996; Erdogdu, 2005). As long as the thermal diffusivity is constant, this first 167 term approach may be easily used to determine the temperature change with Eq. (1) and with the known heat transfer coefficient value: 168

169 $k = \varphi^2 . \alpha / l^2$ at any given position in the infinite slab where φ is the first root of the following 170 equation:

171
$$\cot \varphi = \frac{\varphi}{Bi}$$
(3)

172 At the half thickness of the infinite slab,

173
$$j = \frac{2\sin\varphi}{\varphi + \sin\varphi\cos\varphi}$$
(4a)

174 At the surface of the infinite slab,

175
$$j = \frac{2\sin\varphi\cos\varphi}{\varphi + \sin\varphi\cos\varphi}$$
(4b)

176 With respect to the cooling/heating of the product during the initial 'lag' period (Fo < 0.2), we

177 assumed a straight linear link between T_0 and temperature at time corresponding to Fo = 0.2.

178 **2.2. Bacterial growth modelling**

179 As a primary model, a simple exponential growth without lag time was assumed:

$$N = N_0 e^{\mu t} \tag{5}$$

181 Where *N* is the cell number at time *t*, N_0 is the initial cell number and μ the specific bacterial 182 growth rate at time *t*.

The gamma function corresponds to a comparison between the growth rate of microbial cells growing at given environmental conditions and the optimum growth rate that would be measured at optimal conditions (Zwietering et al., 1992):

186
$$\Gamma = \frac{\mu}{\mu_{opt}}$$
(6)

In the framework of standard calculations aiming to compare processes to each others, a
simplified gamma function depending only on temperature can be derived from the "square
root" model of Ratkowsky et al. (1982) modified by Zwietering et al. (1992)

190
$$\gamma(T) = \left(\frac{T - T_{\min}}{T_{opt} - T_{\min}}\right)^2$$
(7)

191 Where T_{min} is the temperature below which no microbial growth occurs and T_{opt} is the 192 temperature at which the microbial growth is optimal.

If a process has to be intrinsically assessed regardless of the characteristics of the foodstuff, a partial proliferation value may be involved. If the local temperature at which the bacteria are growing is the single considered factor, Mafart (2005) defined a "thermal proliferation value" as:

197
$$f' = \int_0^t \gamma(T) dt$$
(8)

This value has the dimension of a time and corresponds to a time-temperature cycle that would yield the same proliferation ratio than a growth of f' units of time at the optimal and constant temperature (Mafart, 2005).

201 The original differential form of equation (6) is:

202
$$\frac{1}{N}\frac{d(N)}{dt} = \mu(t) = \mu_{opt}\gamma[T(t)]$$
(9)

the solution of which yields:

204
$$\frac{N}{N_0} = \exp\left[\mu_{opt} \int_0^t \left(\frac{T - T_{\min}}{T_{opt} - T_{\min}}\right)^2 dt\right]$$
(10)

This model can be easily combined with heat transfer models permitting the obtainment of an analytic solution yielding the overall model. Note that, even for complex foodstuff shapes, an analytic solution of the model is possible, provided that thermal parameters of equation (1) (jand k) can be empirically determined from a temperature registration and a linear regression of reduced temperature.

The concept of thermal proliferation value may be usefully completed by that of equivalent temperature, which corresponds to the constant temperature that would yield the same proliferation during the duration of a thermal cycle. A cooling/heating process can then be characterised and be compared with others by its duration and its equivalent temperature(Mafart, 2005).

215
$$\gamma(T_{eq})t = f' \tag{11}$$

216 where time is expressed in hours. The combination of this last equation with Eq. (7) yields:

217
$$T_{eq} = T_{\min} + \left(T_{opt} - T_{\min}\right) \sqrt{\frac{f'}{t}}$$
(12)

218 **2.3. Overall model**

The overall model developed in the present study aims to consider the convective heat transfer coefficient and the temperature of the ambient medium when predicting bacterial growth under dynamic conditions of temperature.

222 Combining Eqs. (1) and (7) the obtained time-dependent $\gamma(T)$ function is employed in Eq. (8)

223 in order to express, by integration, f' as a function of t:

224
$$f'(T) = \frac{k(T_{\infty} - T_{\min})^{2}t + 2j(T_{\infty} - T_{\min})(T_{0} - T_{\infty})(1 - e^{-kt}) + \frac{j^{2}}{2}(T_{0} - T_{\infty})^{2}(1 - e^{-2kt})}{k(T_{opt} - T_{\min})^{2}}$$
(13)

The substitution of f' in Eq. (13) by its above-cited expression enables the calculation of the equivalent temperature as follows:

227
$$T_{eq} = T_{\min} + \sqrt{\frac{k(T_{\infty} - T_{\min})^2 t + 2j(T_{\infty} - T_{\min})(T_0 - T_{\infty})(1 - e^{-kt}) + \frac{j^2}{2}(T_0 - T_{\infty})^2(1 - e^{-2kt})}{kt}}$$
(14)

228 The implementation of the Eq. (10) to T_{eq} of the thermal process yields:

229
$$\frac{N}{N_0} = \exp\left[\mu_{opt} \left(\frac{T_{eq} - T_{\min}}{T_{opt} - T_{\min}}\right)^2 t\right]$$
(15)

The overall mathematical model corresponds to the association of these two last equations. The determination of the *j* value at the centre (Eq. (4a)) or at the surface (Eq. (4b)) of an infinite slab allows the calculation of the corresponding T_{eq} values. The parameter *k* is 233 determined from Eq. (3) at any given position in the product and with Bi which includes the 234 convective heat transfer coefficient *h* that will be changed in the experimental validation of 235 the overall model.

236

3. Materials and methods

238 **3.1. Micro-organism and inoculum preparation**

E. coli SOR 201 (isolated from cheese), provided by SOREDAB Laboratory (France), was
stored at -80 °C in nutrient broth supplemented with 50% glycerol. The inoculum was
prepared by subculturing the bacterial strain in 100 mL of nutrient broth (tryptone 10 g/L,
meat extract 5 g/L and sodium chloride 5 g/L. pH 7.2±0.2) at 37 °C on a rotary shaker (100
rpm), subsequently for 8 h and 16 h.

3.2. Experimental setup for the model validation at constant air temperature and changing convective heat transfer coefficient

246 **3.2.1. Growth measurement**

247 Growth curves were determined by the measurement of absorbance changes with a 248 spectrophotometer (Milton Roy, Spectronic 301) at 600 nm wavelength. Absorbance was 249 measured with sterile nutrient broth as a blank. Samples were filled in glass "growth flasks" 250 specially designed for the measurement of the absorbance of the content without sampling. A 251 calibration experiment was done to determine the correlation between viable counts and 252 absorbance data in nutrient broth permitting the estimation of the bacterial concentrations 253 from absorbance values. Samples were incubated at 30 °C in a shaking water bath and 254 bacteria were grown until stationary phase. The optical density was periodically measured and 255 one mL was simultaneously removed from the solution to be analyzed by the plate count 256 method. The experimental dataset was fitted with the exponential model proposed by Juarez 257 Tomas et al. (2002) to fit the calibration equation which can be written as follows:

$$LnN = a(OD)^b \tag{16}$$

259 Where *N* is the bacterial concentration, *OD* is the corresponding optical density (600 nm) 260 measured at time *t* and *a* and *b* are empirical parameters.

Fig. 1 depicts the experimental data and the calibration curve relating *OD* to viable counts. Estimates of parameters *a* and *b* were respectively assessed to 22.8 [22.6 .. 22.9] and 0.090 [0.087 .. 0.093] ($R^2 = 0.999$ and MSE = 0.009).

Francois et al. (2005) demonstrated that a temperature of 4 °C had no significant statistical effect on the linear calibration curve compared to optimal conditions (T 30 °C, pH 7,4 and a_w 0.995) in BHI medium. Consequently, we didn't perform the calibration experiment at other temperatures than 30 °C (the initial product temperature at all the experiments).

268 **3.2.2. Simulation design**

258

269 Five combinations of thickness of an infinite slab, convective heat transfer coefficient and chilling temperature were input (Fig. 2) for the calculation of thermal parameters i and k. A 270 271 simulated growth curve related to each combination was then calculated from Eqs. (14) and (15). An h value of 8 W/(m^2 .K) corresponds to the absence of fan (particularly in unventilated 272 zones or in equipment inside which heat is transferred by natural convection) while an h value 273 of 60 W/(m².K) corresponds to a strong air fan (in the case of forced convection). Moreover, 274 according to Kondjoyan (2006), average heat transfer coefficient values $(W/(m^2.K))$ 275 calculated under different air velocity $(0.2 - 5.0 \text{ m s}^{-1})$ and free-stream turbulence intensity 276 conditions (5 - 40 %) ranged from 1.3 to 42.0 for a circular cylinder and from 2.3 to 60.0 for 277 278 meat products (Beef carcass, pork hindquarter and lamb carcass (loin)). Furthermore, Ben 279 Amara et al. (2004) studied the effect of various factors (air velocity, position, air-product temperature difference) on the transfers during cooling with a low air velocity (< 0.2 m/s), of 280 an in-line stack of spheres and measured h values ranging from 8 to 19 W/(m^2 .K) for air 281 velocity varying from 0.03 to 0.19 m s⁻¹. 282

283 **3.2.3.** Conditions of growth for the validation of the model

Corresponding to each combination of slab thickness and convective heat transfer coefficient, cooling profiles and bacterial growth were simulated at the centre and at the surface of an infinite slab shaped product. The product thermal diffusivity and thermal conductivity values input in the calculations were assumed to be equal to those of water determined at 25 °C, i.e. $1.43.10^{-7}$ m²/s and 0.6 W/(m.K) respectively.

289 Furthermore, input μ_{opt} , T_{min} and T_{opt} values of E. coli SOR 201 were respectively equal to 290 2.66 h⁻¹, 3.28 °C and 42.03 °C in nutrient broth. These values were estimated from forty six 291 growth kinetics conducted at 11 constant temperatures ranging from 10 °C to 46 °C. Experimental datasets were fitted and growth curve parameters (maximum growth rate (μ_{max}), 292 293 lag time, initial and maximum population densities) were estimated from the primary growth 294 model of Baranyi and Roberts (1994). The obtained μ_{max} values were fitted with the 295 secondary cardinal model (Rosso et al., 1995) in order to estimate the optimal growth rate and 296 the cardinal temperatures of *E. coli* SOR 201 (see Fig. A2 in the appendix).

297 In order to validate the overall mathematical model developed in the present work, 298 experiments were conducted under a changing temperature program which corresponds to the 299 simulated cooling profiles of the surface or the centre of the product. All the prepared material 300 was pre-chilled/heated to the initial temperature (30 °C). Subculture was diluted to provide an inoculation level ranging from 10^6 to 10^7 CFU/mL at the starting of the test. Samples were 301 302 filled in glass "growth flasks" allowing the measurement of the absorbance of the content, 303 during the experiment, without sampling. Their shaking was guaranteed by a magnetic 304 shaking table. Samples were instantly incubated and periodically removed so as to measure 305 optical densities (at 600 nm) in the course of the experiment. Experiments were carried out in 306 triplicate. The chilling was monitored with a refrigerated and heating circulator (FP40-HE, 307 Julabo Labortechnik GmbH, Germany) allowing a temperature stability of ±0.01 °C.

308 3.3. Experimental setup for the model validation at changing air temperature and 309 constant convective heat transfer coefficient

For a further validation of the model, more complicated temperature scenarios were tested assuming alternated cooling and heating stages. Moreover, an inoculation level ranging from 10^3 to 10^4 CFU/mL was used in order to consider more realistic bacterial concentrations encountered in food industry processes.

314 Three different ambient air temperature scenarios, drawn from real refrigerated food 315 processes, were tested (cf. Table 2).

Corresponding to each air temperature scenario, temperature profiles and bacterial growth were simulated at the centre and at the surface of an infinite slab shaped product. At all the tested temperature scenarios, the initial product temperature, the product thickness and the convective heat transfer coefficient were respectively equal to 15 °C, 0.12 m and 8 W/(m².K). Input μ_{opt} , T_{min} and T_{opt} values of *E. coli* SOR 201 are mentioned above. Typical beef meat thermal diffusivity and thermal conductivity values, respectively equal to 1.25.10⁻⁷ m²/s and 0.42 W/(m.K), were input in the calculations.

323 Experiments were conducted under thermal programs which corresponded to the simulated 324 temperature profiles of the surface or the centre of the product. Subculture was diluted, 325 samples were filled in glass "growth flasks", instantly incubated and periodically removed so 326 as to perform the viable count measurement in the course of the experiment. Experiments 327 were carried out in duplicate. The thermal program was monitored with the refrigerated and 328 heating circulator (FP40-HE, Julabo Labortechnik GmbH, Germany). At each sampling time, 329 1-mL aliquots were aseptically removed from each "growth flask", serially diluted in tryptone 330 salt broth and plated on nutrient agar (15 g/L) with a double layer. Petri dishes were incubated 331 at 37 °C for 24 h and colonies were counted.

332 **3.4.** Validation and assessment of the quality of the overall model

333 Model accuracy was assessed by the estimation of confidence bands of predictions by using 334 the bootstrap percentile method (Efron and Tibshirani, 1993). Forty six growth kinetics were 335 performed in nutrient broth at 11 constant temperatures ranging from 10 °C to 46 °C (data not 336 shown). Bootstrap of each kinetic was made in order to take the experimental errors of 337 kinetics into account. The appropriate residuals of each kinetic were drawn with replacement. 338 Twenty five thousands bootstrap set of primary parameters were obtained. Each set of 339 bootstrapped μ_{max} values were used to fit the secondary model. Then bootstrapped values of 340 parameters T_{min} , T_{opt} and μ_{opt} were used to predict the bacterial growth with the overall model. 341 Secondary observed residuals were drawn with replacement and added to the μ predicted 342 value. Primary residuals were added to the predicted kinetics to consider the experimental 343 error of cell number estimation. Twenty five thousands bootstrapped growth kinetics were 344 obtained for each validation experiment and sorted in ascending order at each calculation 345 time. The quartiles 2.5% and 97.5% of the sorted bootstrapped kinetics were taken to give the 346 inferior and superior limits. These points were linked to give an approximation of the 95 347 percent confidence bands of the predicted growth kinetics. To validate the assumptions made 348 and the model, less than 5% of the points must fall outside the confidence bands.

With regard to the assessment of the quality of the overall model predictions various statistical criteria were calculated at all the tested conditions of validation experiments. Correlation coefficients (R) between observations and predictions were calculated using the 'corrcoef' function of MATLAB 6.5. The correlation coefficient is related to the covariance *cov* by:

354
$$R(i,j) = \frac{\operatorname{cov}(i,j)}{\sqrt{\operatorname{cov}(i,i)\operatorname{cov}(j,j)}}$$
(17)

355 where i is the observations index and j is the variables index.

Bias factor B_f (Eq. (18)) and Accuracy factor A_f (Eq. (19)) were calculated as proposed by Jeyamkondan et al. (2001). These factors were initially introduced by Ross (1996) but here, the predicted values are normalized.

359
$$B_f = 10^{\sum \log(P/O)/n}$$
 (18)

360
$$A_f = 10^{\sum |\log(P/O)|/n}$$
 (19)

361 where *O* and *P* are observed and predicted microbial populations in \log_{10} CFU/mL and *n* is 362 the number of observations. The bias factor indicates the relative average deviation of 363 predicted and observed bacterial growth. However it has to be kept in mind that this deviation 364 does not directly concern the size of the population, but its logarithmic transformation which 365 reduces the effect of outliers.

A bias factor of 1 indicates perfect agreement between observed and predicted values. 366 However, $B_f > 1$ or < 1 indicates that the model predicts N upper than or lower than observed 367 values. For example, $B_f = 1.1$ means that predictions are on average upper than observed 368 values by 10%. The accuracy factor gives indication of the spread of the results about the 369 370 predicted value. An accuracy factor of 1 represents perfect agreement between observed and 371 predicted values. This parameter quantifies the difference between observed and predicted values. For example, $A_f = 1.25$ indicates that the average deviation of the predicted values 372 from the observed values is 25%. It has to be kept in mind that this deviation does not directly 373 374 concern the size of the population, but its logarithmic transformation. 375 4. Results

4.1. Model validation at constant air temperature and changing convective heat transfer coefficient

4.1.1. Growth simulation

Thermal programs tested at the validation stage were utilized at five different combinations of product thickness (E), convective heat transfer coefficient (h) and refrigeration temperature 381 (T_{∞}) (Fig. 2).

382 The obtained cooling profiles and growth predictions are presented in Fig. 3. As a rule, 383 bacterial growth kinetics were faster at the product centre than at its surface. In cases of 384 lowest thickness, simulated computing profiles (1c and 2c) were practically identical leading 385 to the same bacterial growth predictions (1g and 2g) at the centre and at the surface of the 386 product. In fact, in these two experiments the product thickness was sufficiently low to 387 prevent a clear observation of an internal temperature gradient and the internal heat resistance 388 may had been neglected. In contrast, the difference between simulated theoretical temperature 389 kinetics at the centre and the surface of the product were more marked in the cases of the 390 highest thickness leading to an important thermal gradient within the product (3c and 4c). For 391 that matter, the most important differences between internal and surface growth kinetics were 392 obtained in these two cases (3g and 4g), particularly in the case of low heat transfer 393 coefficient.

On the other hand, additional simulated growth curves at constant temperatures equal to T_{∞} were presented in Fig. 3. The aim of these further experiments was to compare the bacterial growth that really occurs when temperature dynamic changes at the centre and at the surface of the cooled product are considered, with the growth that would occur if external and internal resistances were neglected.

399 **4.1.2. Validation results**

Each validation experiment regarding each (T_{∞} , h, E) combination (Fig. 2) was conducted under two different refrigeration programs which corresponded to the simulated cooling of the surface and the centre of the infinite slab-shaped product yielding a total of eight validation tests. These tests lasted 24 hours with an initial temperature T_0 of 30 °C. In order to validate the overall mathematical model, Fig. 4 depicts predicted and observed *E. coli* SOR 201 growth during the simulated cooling at the centre or the surface of the product for the five 406 cases presented in Fig. 2. A fair agreement between predicted and observed growth can be 407 noted, and the observed growth data of *E. coli* SOR 201 were found to be adequately 408 predicted by the overall mathematical model. For each predicted growth kinetic, 95 percent 409 confidence bands calculated with bootstrap method are also presented in Fig. 4. All the 410 experimental data fell inside the confidence bands showing that the overall model was 411 successfully validated at the tested conditions.

412 On the other hand, the quality of the overall model prediction was assessed by the calculation 413 of correlation coefficient, B_f and A_f (see Table 3). The correlation coefficients were higher 414 than 0.975 showing that the bacterial growth was satisfactorily predicted by the overall 415 model. At all the instances, bias factors ranged from 0.98 to 1.00 indicating that on average, 416 the observed growth was at the most 2% higher than the predicted growth and that the overall 417 predictions agreed well with observed data with a slight under-prediction tendency by the 418 model. In all the tested conditions, the percentage of predicted values which were different 419 (either above or below) than the observed values was at the most equal to 5% as can be noted 420 from Af values ranging from 1.01 to 1.05.

Agreement between model predictions and experimental validation results was also assessed by plotting predicted bacterial growth versus observed bacterial growth (Fig. 5). A perfect agreement between predicted and measured growth was observed for 30.80% of experimental data. A percentage of 25.36% of the observed–predicted values' pairs were laying under the line of equivalence while 43.84% were laying above the line of equivalence.

426 4.2. Model validation at changing air temperature and constant convective heat transfer 427 coefficient

428 **4.2.1. Growth simulation**

Fig. 6 illustrates the simulated thermal profiles and bacterial growth kinetics according to theconditions presented in Table 2 and §3.3. Thermal and bacterial growth simulation results

431 showed important differences of temperature profiles and growth between the product centre, 432 the product surface and the ambient air. During heating, the highest bacterial growth was 433 observed when simulations were carried out at air temperature, followed by the product's 434 surface and then by the product's centre. Conversely, an opposite trend was observed during 435 cooling. From a safety point of view, neglecting heat transfer phenomena that occur inside the 436 product and between the ambient air and the product is more dangerous at cooling stages than 437 at heating stages. Nevertheless this hazard depends on the temperature and duration history of 438 the cooling/heating stages. Consequently it's very important to take into account the actual 439 temperature of the product surface or centre rather than the ambient air temperature for a 440 reliable bacterial growth prediction.

441 **4.2.2. Validation results**

442 Validation results regarding the three tested ambient scenarios are presented in figures 7 and 443 8. The observed growth data of *E. coli* SOR 201 were found to be adequately predicted by the 444 overall mathematical model. On the other hand, less than 5% of the experimental data fell 445 outside the 95 percent confidence bands showing that the overall model was successfully 446 validated at the tested conditions. Table 4 presents the statistical criteria related to the data of 447 validation at changing air temperature and shows correlation coefficients higher than 0.944 at 448 all the tested conditions. Bias factors obtained at all the assays were higher than 1 showing a 449 slight over-prediction tendency by the model. A_f values (lower than 1.13 at all the instances) 450 indicate that the overall predictions agreed well with observed data. Fig. 8 shows predicted 451 bacterial growth versus observed bacterial growth and confirms that the overall model was 452 successfully validated, with a slight over-prediction tendency, for the tested dynamic 453 refrigeration cycles.

454 **5. Discussion**

455 Traditionally, when simulating a bacterial growth during a product cooling or heating, 456 predictive microbiology took only the ambient air temperature into account, ignoring delays 457 and temperature gradients due to external and internal thermal resistances linked to the effects 458 of the medium thickness and of the convective heat transfer coefficient on the rate of heat 459 transfer. All the studies cited in Table 1 have evaluated the prediction of bacterial growth 460 under dynamic temperature conditions taking into account only the temperature of the 461 cooling/heating medium. Assuming that the bacterial growth directly occurs at the 462 temperature of air is not valid. In fact, the local temperature at any given position in the product depends upon both T_{∞} and h. In the present study, predictive microbiology was 463 464 combined with heat transfer phenomena in order to develop an overall mathematical model 465 describing the effect of the ambient temperature and the convective heat transfer coefficient 466 on bacterial growth. The proposed method in this work is different than those in previous 467 studies which combined predictive microbiology and heat transfer (Alavi et al., 2001; 468 Amezquita et al., 2005; Bellara et al., 2000; Corradini et al., 2006). An experimental method 469 was implemented in order to validate the model results. Thermal profiles were firstly 470 simulated at the centre and at the surface of the infinite slab shaped product. Then, 471 experiments were conducted under a changing temperature program corresponding to the 472 simulated temperature kinetics. The validation of the overall model was performed by the 473 comparison of the measured bacterial growths with model predictions at constant ambient air 474 temperature and changing convective heat transfer coefficient and product thickness (five 475 different combinations of product thickness, convective heat transfer coefficient and cooling 476 air temperature were tested), then at changing ambient air temperature and fixed convective 477 heat transfer coefficient and product thickness (three different ambient air scenarios assuming 478 alternated cooling and heating stages, drawn from real refrigerated food processes, were 479 tested).

480 As expected, the results of the computer simulation related to single cooling stage 481 experiments showed that the bacterial growth kinetics were faster at the product centre than at 482 its surface. Moreover, the importance of the impact of the convective heat transfer coefficient 483 and of the product thickness on the bacterial growth during the cooling of an infinite slab 484 shaped product by pulsed air was pointed out. As an example, at the product half thickness, the level of bacterial growth accomplished after 5 hours of cooling with $h = 8 \text{ W}/(\text{m}^2\text{.K})$ (case 485 3) was the same after 16.5 hours with $h = 60 \text{ W/(m}^2\text{.K})$ (case 4). For these cases the product 486 487 thickness was the same and the cooling air temperature was in case 3 4°C lower than in case 488 4. Similarly, at product half thickness, the cooling time needed to reach a same bacterial 489 growth with low or high product thickness (1 cm in case 2 and 6 cm in case 4) was estimated 490 to 17.5 hours and 8 hours, respectively, for the same convection level (60 $W/(m^2.K)$). The 491 slowest simulated bacterial growth was observed with intermediate product thickness and 492 convective heat transfer coefficient (case 5). Moreover, it obviously appears that the validity 493 of the assumption of an instantaneously thermal equilibrium between the product and the 494 cooling medium with regard to bacterial growth is depending on the level of convection. In 495 fact, predicted growth kinetics at the surface of the product were close to those predicted at T_{∞} for high heat transfer coefficients (*h*) equal to 60 $W/(m^2.K)$, which corresponds to a strong air 496 497 fan (Fig. 3: 2g and 4g). At this instance, neglecting the external heat resistance may be accepted particularly for low product thickness (1 cm) where there's no internal heat 498 resistance too. Oppositely, for low heat transfer coefficients (h) equal to 8 W/(m^2 .K), which 499 500 corresponds to the absence of fan, (Fig. 3: 1g and 3g) important dissimilarities between 501 predicted growth kinetics at the surface of the product and at T_{∞} may be observed. Indeed, 502 assuming no external heat transfer resistance is not valid especially for high product thickness 503 of 6 cm (Fig. 3: 3g) where the bacterial growth that occurs when the product is cooled from T_0 to T_{∞} was clearly higher than that at an immediately reached temperature T_{∞} . In this case, a 504

505 difference of 1.35 $\log_{10}(CFU/mL)$ between the bacterial populations at the product surface 506 and at T_{∞} was reached after 24 hours of growth. Besides, using the bootstrap percentile 507 method for the estimation of confidence bands of predictions, the model was successfully 508 validated at all the tested conditions.

509 Concerning the results related to alternated cooling and heating stage experiments, the model 510 was successfully validated at more complicated ambient air scenarios and lower inoculation 511 levels by plate count measurement method. These results showed that, in predictive 512 microbiology, assuming an instantaneously thermal equilibrium between the product and the 513 ambient medium is not valid and may have large consequences on risk assessment of 514 refrigerated food processes (see Fig. 9).

515 To assess the quality of the overall model, predicted bacterial growth was compared to 516 observed growth according to several statistical criteria related to the data of validation. Our 517 results pointed out a good agreement between predicted and observed growth.

518 On the other hand, in the overall model, as a primary bacterial model, a simple exponential 519 growth without lag time was assumed. In other words, it is supposed that the bacterial growth 520 occurred without delay when the product temperature was continuously changing. Our 521 assumption is in agreement with several previous studies. Although the fact that organisms 522 need to adapt to the new temperature, so that they go through a lag phase caused by the stress 523 of the temperature shift, was largely noticed in literature (Amezquita et al., 2005; Baranyi et 524 al., 1995; Koutsoumanis, 2001; Zwietering et al., 1994), the lag phase duration was rarely 525 considered in predictive models. In accordance with our work, no further delay occurring after 526 temperature shifts, once a cell population is growing exponentially, was frequently assumed 527 (Baranyi et al., 1995; Bovill et al., 2000; Koutsoumanis et al., 2006). Although, Swinnen et al. 528 (2005) demonstrated that temperature shifts crossing a lag/no lag transition zone (positioned 529 more or less between 22.78 and 23.86 °C for E. coli K12 MG1655) will cause an intermediate 1 lag phase, we consider that neglecting contingent intermediate lag phase by our model may be a valid approach. In fact, simulated thermal profiles at product surface or centre due to heat transfer phenomena (see Fig. 3 and Fig. 6) progressively changed with time and cannot be regarded as instantaneous temperature shifts with given amplitude which may generate intermediate lag phases.

535 Paradoxically, the complexity of foods' shapes and the lack of knowledge about their physical 536 properties dictate the utilization of simple model. We took as an example the case of infinite 537 slab, but the model can be generalised to complex shapes. A classical and relevant approach is 538 of course, the implementation of numerical modelling. Another approach is related to the 539 well-known Ball method (Ball, 1923) with its two empirical parameters, for heat treatment 540 processes calculations. Because foodstuffs shapes are complex and because their thermal 541 properties are often unknown, it can be relevant to implement a simple model including only 542 two parameters (j and k of Eq. (1)) which can be easily empirically estimated from a simple 543 temperature registration and a simple linear regression of the reduced temperature (which is 544 linearised from a logarithmic transformation). Note that errors which can be generated by 545 "simplistic" heat transfer models are minor compared to errors which are linked to the 546 "biological background". Moreover, the overall model can be used for any bacterial strain 547 having known growth parameters T_{min} , T_{opt} and μ_{opt} . Accordingly, the proposed model can be 548 used for designing safe cooling or heating processes and may be considered as a very useful 549 tool for risk assessment regarding food safety and process optimisation.

550 6. Appendix

551 Equation of the the infinite series given by Carslaw and Jaeger (1986):

552
$$\frac{T_{\infty} - T}{T_{\infty} - T_0} = \sum_{n=1}^{\infty} \frac{2\sin\varphi_n}{\varphi_n + \sin\varphi_n \cos\varphi_n} \cos\left(\varphi_n \frac{x}{x_{\max}}\right) \exp\left(-\varphi_n^2 F_0\right)$$
(20)

553 with x_{max} is half-thickness for an infinite slab and φ_n are the roots of the equation $\cot \varphi = \frac{\varphi}{Bi}$.





Fig. A1. Typical cooling curve (Becker and Fricke, 2004)

556



558 Fig. A2. Fit of the cardinal model on μ_{max} values measured in nutrient broth (×). The dashed 559 line denotes the fitted model on the experimental data.

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684	979.

687	Figure captions
688	
689	Fig. 1.
690	
691	Calibration curve between viable counts and absorbance data depicted with solid line.
692	Experimental data measured at 30°C in nutrient broth are marked with (o).
693	
694	Fig. 2.
695	
696	Experimental design implemented for the validation of the overall model at different
697	combinations (mentioned with numbers from 1 to 5) of product thickness (E), convective heat
698	transfer coefficient (h) and refrigeration temperature (T_{∞}) .
699	
700	Fig. 3.
701	
702	Cooling scenarios (from 1c to 5c) and bacterial growth curves (from 1g to 5g) obtained from
703	simulation of the overall model at the five cases of the experimental design. Symbols in
704	predicted cooling profiles: temperature of product centre (line —) and temperature of product
705	surface (line — \cdot —). Symbols in predicted growth curves: bacterial growth at product centre
706	(line —), bacterial growth at product surface (line — \cdot —) and bacterial growth that occurs at
707	T_{∞} (line).
708	
709	Fig. 4.
710	
711	Comparison of predicted and observed Escherichia coli SOR 201 growth during cooling. a:
712	case1 at the centre or the surface of the product. b : case2 at the centre or the surface of the
713	product. <i>c</i> : case3 at the product centre. <i>d</i> : case3 at the product surface. <i>e</i> : case4 at the product
714	centre. f : case4 at the product surface. g : case5 at the product centre. h : case5 at the product
715	surface. Symbols in experimental data: o, \Box , Δ . Predicted growth curves estimated by the
716	overall model are presented with (line -). 95 percent confidence bands obtained with
717	bootstrap method are presented with (line $$).

720 Fig. 5.

721

Predicted bacterial growth from the overall model versus observed bacterial growth obtained with constant air temperature. Symbols: \Box (case 1), o (case 2). Symbols related to product surface experiments: * (case 3), Δ (case 4), \diamond (case 5). Symbols related to product centre experiments: • (case 3), + (case 4), x (case 5). The line of equivalence between predicted and observed growth is marked with (line –).

727

728 Fig. 6.

729

Thermal profiles (from 1c to 3c) and bacterial growth curves (from 1g to 3g) obtained by simulation of the overall model at the three ambient air scenarios. Symbols in predicted cooling profiles: temperature of product centre (line —) and temperature of product surface (line — · —). Symbols in predicted growth curves: bacterial growth at product centre (line — · —), bacterial growth at product surface (line — · —) and bacterial growth that occurs at T_{∞} (line ……).

736

737 Fig. 7.

738

Comparison of predicted and observed *Escherichia coli* SOR 201 growth during thermal processing at changing air temperature. *a*, *c* and *e* depict the model validation results at the product centre according to cycle N°1, cycle N°2 and cycle N°3, respectively. *b*, *d* and *f* depict the model validation results at the product surface according to cycle N°1, cycle N°2 and cycle N°3, respectively. Symbols in experimental data: o, \Box . Predicted growth curves estimated by the overall model are presented with (line –). 95 percent confidence bands obtained with bootstrap method are presented with (line –).

746

747 Fig. 8.

Predicted bacterial growth from the overall model versus observed bacterial growth obtained with changing air temperature. Symbols related to product surface experiments: \Box (Cycle N°1), * (Cycle N°2), Δ (Cycle N°3). Symbols related to product centre experiments: o (Cycle N°1), • (Cycle N°2), + (Cycle N°3). The line of equivalence between predicted and observed growth is marked with (line –).

- 753 Fig. 9.
- 754 Comparison of the bacterial growth prediction at ambient temperature according to cycle N°1
- with the model validation results at product's centre (a) and at product's surface (b). Symbols
- in experimental data: o, □. Symbols in predicted growth curves: bacterial growth at product's
- surface or centre (line –), bacterial growth that occurs at T_{∞} (line). 95 percent confidence
- band of predictions at T_{∞} obtained with bootstrap method is presented with (line --).



763 Fig. 1.









783 Fig. 3.



















803 Table 1

804 List of previous works dealing with models predicting the bacterial growth under dynamic

805 temperature conditions

/ Model	Secondary model	Solution method	Validation conditions	R
nd Roberts aranyi and 4).	Quadratic polynomial model.	Numerical solution by the fourth order Runge–Kutta method.	Rates of change of T ranging from 1.7° C.h ⁻¹ to a virtually instantaneous change: cooling from 25°C to -2, 2, 5 or 10°C and heating from 2°C to 25°C.	Bovil
istic model.	Arrhenius equation.	Numerical solution by the fourth order Runge–Kutta method.	Various types of a dynamic temperature history with various intervals were studied for of <i>Escherichia coli</i> 1952 growth prediction.	Fujik 2004
nd Roberts aranyi and 4).	A modified Ratkowsky equation (Zwietering et al., 1991).	Numerical solution by the fourth order Runge–Kutta method.	Growth of <i>Salmonella Enteritidis</i> in egg yolk under varying temperature profiles (exponential and linear cooling, exponential heating and sinusoidal temperatures).	Gumu al., 20
form of the odel (Gibson	A modified Ratkowsky equation (Zwietering et al., 1991).	Numerical solution by the fourth order Runge–Kutta method.	Growth of <i>Clostridium perfringens</i> in cooked ground beef under fluctuating temperature conditions between 30°C and 45°C (square waved) and under continuous temperature changes from 51°C to 10°C (linear and exponential cooling).	Huan

- 807 Table 2
- 808 Tested temperature scenarios for the validation of the model at changing air temperature and
- 809 constant convective heat transfer coefficient equals to $8 \text{ W}/(\text{m}^2.\text{K})$

Stage of the cycle	Temperature (°C)	Duration (h)
Cycle N° 1		
Storage in a cold room	2.5	24
Refrigeration stopped due to an accidental failure of the installation	21	24
Repaired breakdown and remaining product in the cold room	2.5	24
Cycle N° 2		
Industrial storage and transport	9.5	18
Household doorstep delivery	30	4
Storage in refrigerator	9.5	24
Product on the table	30	2
Remaining product in the refrigerator	9.5	18
Cycle N° 3		
Storage and transport	5	24
Storage in the refrigerated cabinet	12	24
Household doorstep delivery	25	4
Storage in refrigerator	8	24

- 811 Table 3
- 812 Statistical criteria related to the data of validation at constant air temperature and changing
- 813 convective heat transfer coefficient
- 814

Test conditions	D	D	1
Test conditions	Λ	D_f	A_{f}
Case 1	0.996	0.98	1.03
Case 2	0.996	0.99	1.01
Case 3	0 087	0.08	1.04
at product centre	0.987	0.98	1.04
Case 3	0 087	0 00	1.02
at product surface	0.767	0.99	1.02
Case 4	0 976	0 99	1.05
at product centre	0.770	0.77	1.05
Case 4	0.986	0 99	1.03
at product surface	0.980	0.77	1.05
Case 5	0 975	0 99	1.03
at product centre	0.975	0.77	1.05
Case 5	0 99/	1	1.01
at product surface	0.774	1	1.01

- 817 Table 4

818 Statistical criteria related to the data of validation at changing air temperature and constant 819 convective heat transfer coefficient equals to $8 \text{ W/(m}^2.\text{K})$

Test conditions	R	B_{f}	A_f
Cycle 1 at product centre	0.991	1.05	1.05
Cycle 1 at product surface	0.992	1.04	1.05
Cycle 2 at product centre	0.963	1.08	1.08
Cycle 2 at product surface	0.986	1.06	1.06
Cycle 3 at product centre	0.944	1.13	1.13
Cycle 3 at product surface	0.964	1.09	1.09